

# **Very long baselines with a superbeam**

Milind Diwan

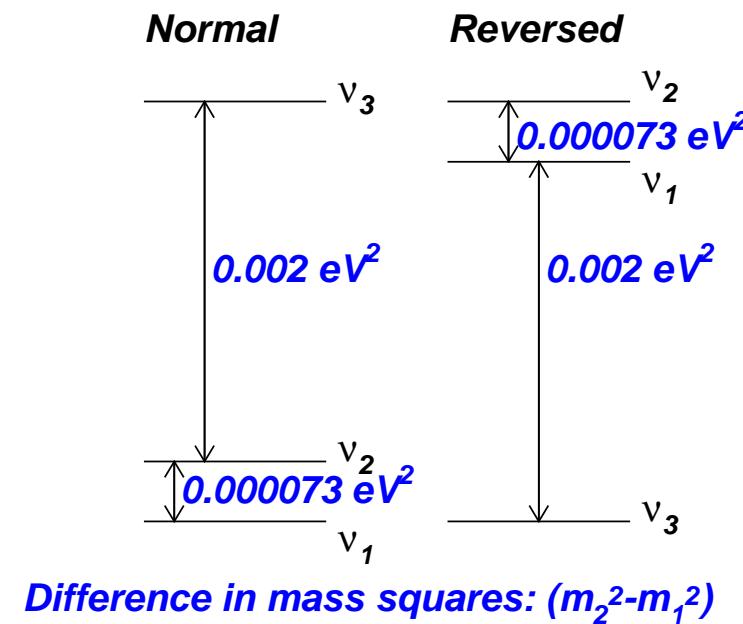
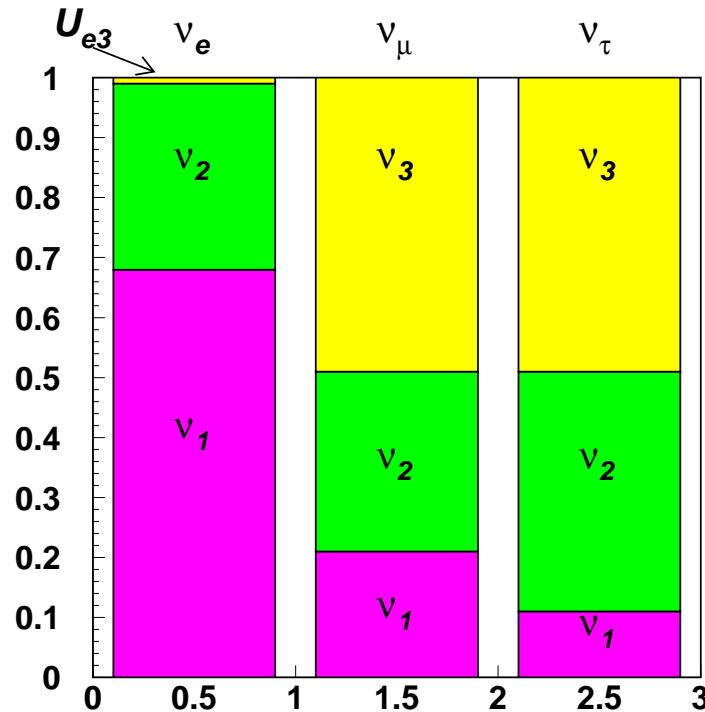
FOR BNL Neutrino Working Group.

December 1, 2003

University of California, Los Angeles

Wide Band Conventional Beam from BNL to the  
Homestake Laboratory.

# Big Picture



Very long baselines with a superbeam

# Neutrino Physics so far

- Evidence for Neutrino flavor change
  - Atmospheric neutrinos: SuperK
  - Solar: SNO, All previous radio-chemical measurements.
  - KamLAND: Confirm the solar LMA solution.
  - Limits on parameters from many accelerator and reactor exp.
  - LSND: To be addressed by mini-boone.
- Direct Neutrino mass
  - Oscillations: Neutrinos definitely have mass.
  - Tritium beta-decay:  $< 2.8$  eV.
  - Double beta decay: mass  $< 0.3$  eV if Majorana.
  - Astrophysics: Large Scale Structure  $< 1$  eV.
- Number of Neutrinos
  - Z width:  $2.981 \pm 0.008$  active types
  - Limits on sterile neutrinos from solar, atmospheric results.
  - Big Bang Nucleosynthesis: 3 active neutrinos.

# Neutrino Physics: Oscillations

Assume a  $2 \times 2$  neutrino mixing matrix.

$$\begin{pmatrix} \nu_a \\ \nu_b \end{pmatrix} = \begin{pmatrix} \cos(\theta) & \sin(\theta) \\ -\sin(\theta) & \cos(\theta) \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix} \quad (1)$$

$$\begin{aligned} \nu_a(t) &= \cos(\theta)\nu_1(t) + \sin(\theta)\nu_2(t) \\ P(\nu_a \rightarrow \nu_b) &= |<\nu_b|\nu_a(t)>|^2 \\ &= \sin^2(\theta)\cos^2(\theta)|e^{-iE_2t} - e^{-iE_1t}|^2 \end{aligned} \quad (2)$$

Sufficient to understand most of the physics:

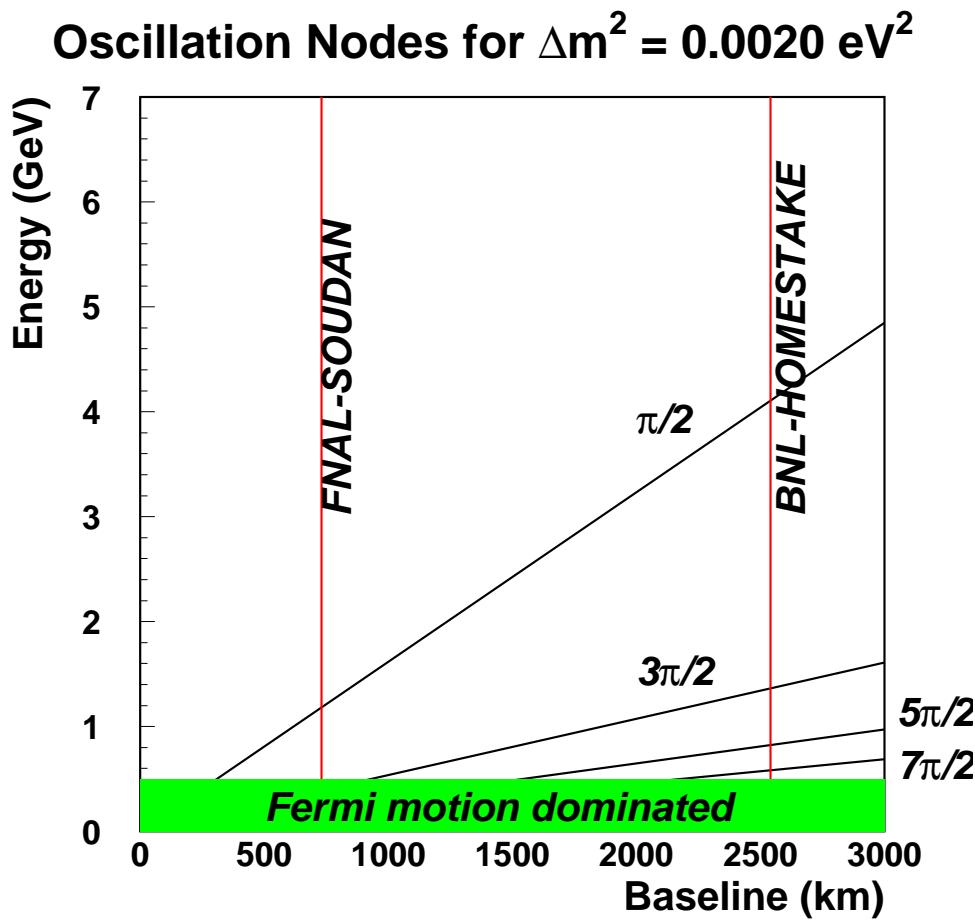
$$P(\nu_a \rightarrow \nu_b) = \sin^2 2\theta \sin^2 \frac{1.27((m_2^2 - m_1^2)/eV^2)(L/km)}{(E/GeV)}$$

$$P(\nu_a \rightarrow \nu_a) = 1 - \sin^2 2\theta \sin^2 \frac{1.27(\Delta m^2/eV^2)(L/km)}{(E/GeV)}$$

Oscillation nodes at  $\pi/2, 3\pi/2, 5\pi/2, \dots (\pi/2)$ :  
 $\Delta m^2 = 0.002eV^2$ ,  $E = 1GeV$ ,  $L = 618km$ .

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# Matter Effect



- Large effects: Multiple oscillation nodes.
- Low cross section at low energies
- Fermi motion limits resolution at low energies: wide band beam ( $0.5 \rightarrow 8 \text{ GeV}$ ).
- $\Delta m^2 \approx 0.002 \text{ eV}^2$ : Baseline  $> 2000 \text{ km}$ .

# Neutrino Physics: $3 \times 3$ Formulation

Bill Marciano, hep-ph/0108181

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} \quad (3)$$

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} \quad (4)$$

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# Neutrino Physics: the difficult stuff

$$\begin{aligned}
 P(\nu_\mu \rightarrow \nu_e) = & 4(s_2^2 s_3^2 c_3^2 + J_{CP} \sin \Delta_{21}) \sin^2 \frac{\Delta_{31}}{2} \\
 & + 2(s_1 s_2 s_3 c_1 c_2 c_3^2 \cos \delta - s_1^2 s_2^2 s_3^2 c_3^2) \sin \Delta_{31} \sin \Delta_{21} \\
 & + 4(s_1^2 c_1^2 c_2^2 c_3^2 + s_1^4 s_2^2 s_3^2 c_3^2 - 2s_1^3 s_2 s_3 c_1 c_2 c_3^2 \cos \delta) \\
 & \quad - J_{CP} \sin \Delta_{31}) \sin^2 \frac{\Delta_{21}}{2} \\
 & + 8(s_1 s_2 s_3 c_1 c_2 c_3^2 \cos \delta - s_1^2 s_2^2 s_3^2 c_3^2) \sin^2 \frac{\Delta_{31}}{2} \sin^2 \frac{\Delta_{21}}{2}
 \end{aligned} \tag{5}$$

No matter effects in above formula

$$\Delta_{31} \equiv \Delta m_{31}^2 L / 2E_\nu$$

$$\Delta_{21} \equiv \Delta m_{21}^2 L / 2E_\nu$$

$$J_{CP} \equiv s_1 s_2 s_3 c_1 c_2 c_3^2 \sin \delta \quad (6)$$

$$A \equiv \frac{P(\nu_\mu \rightarrow \nu_e) - P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)}{P(\nu_\mu \rightarrow \nu_e) + P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)} \quad (7)$$

To leading order in  $\Delta_{21}$  (assumed to be small), one finds

$$\begin{aligned} P(\nu_\mu \rightarrow \nu_e) &\simeq 4s_2^2 s_3^2 c_3^2 \sin^2 \frac{\Delta_{31}}{2} + \mathcal{O}(\Delta_{21}) \\ A &\simeq \frac{J_{CP} \sin \Delta_{21}}{s_2^2 s_3^2 c_3^2} \simeq \frac{2s_1 c_1 c_2 \sin \delta}{s_2 s_3} \left( \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \right) \frac{\Delta m_{31}^2 L}{4E_\nu} + \mathcal{O}(\Delta_{21}^2) \end{aligned}$$

## $\nu_\mu \rightarrow \nu_e$ with matter effect

Approximate formula (Lindener, Huber et al.)

$$\begin{aligned}
 P(\nu_\mu \rightarrow \nu_e) \approx & \sin^2 \theta_{23} \frac{\sin^2 2\theta_{13}}{(\hat{A} - 1)^2} \sin^2((\hat{A} - 1)\Delta) \\
 & + \alpha \frac{8J_{CP}}{\hat{A}(1 - \hat{A})} \sin(\Delta) \sin(\hat{A}\Delta) \sin((1 - \hat{A})\Delta) \\
 & + \alpha \frac{8I_{CP}}{\hat{A}(1 - \hat{A})} \sin(\Delta) \cos(\hat{A}\Delta) \sin((1 - \hat{A})\Delta) \\
 & + \alpha^2 \frac{\cos^2 \theta_{23} \sin^2 2\theta_{12}}{\hat{A}^2} \sin^2(\hat{A}\Delta)
 \end{aligned} \tag{8}$$

$$J_{CP} = 1/8 \sin \delta_{CP} \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23}$$

$$I_{CP} = 1/8 \cos \delta_{CP} \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23}$$

$$\alpha = \Delta m_{21}^2 / \Delta m_{31}^2, \Delta = \Delta m_{31}^2 L / 4E$$

$$\hat{A} = 2VE / \Delta m_{31}^2$$

## Comments about matter effect

$V = \sqrt{2}G_F n_e$ .  $n_e$  is the density of electrons in the Earth.

$$\hat{A} \approx 7.6 \times 10^{-5} \times (D/gm/cm^3) \times (E_\nu/GeV)/(\Delta m_{31}^2/eV^2),$$

Also recall  $\Delta m_{31}^2 = \Delta m_{32}^2 + \Delta m_{21}^2$ .

- This is a very approximate equation, not applicable below the first maximum.
- First term has the effect of  $\sin^2 2\theta_{13}$  and matter.
- Second and third terms have effects of CP.
- Term with  $J_{CP}$  changes sign for  $(Anti - \nu_\mu) \rightarrow (Anti - \nu_e)$
- Last term is almost independent of  $\Delta m_{31}^2$  and is purely dominated by the solar  $\Delta m_{21}^2$

## Some Observations

If performing an appearance experiment ( $\nu_\mu \rightarrow \nu_e$ ) or ( $\nu_e \rightarrow \nu_\mu$ ) around  $\pi/2$  node then

- a) Difficult to avoid matter effect at accelerator energies.
- b) Any reasonable accelerator based experimental setup has sizable contribution from all 4 effects

Matter effect or mass hierarchy

$$\theta_{13}$$

$$\delta_{CP}$$

$$\Delta m_{21}^2$$

- c) To disentangle must have several data points on the oscillation curve (different L or E).

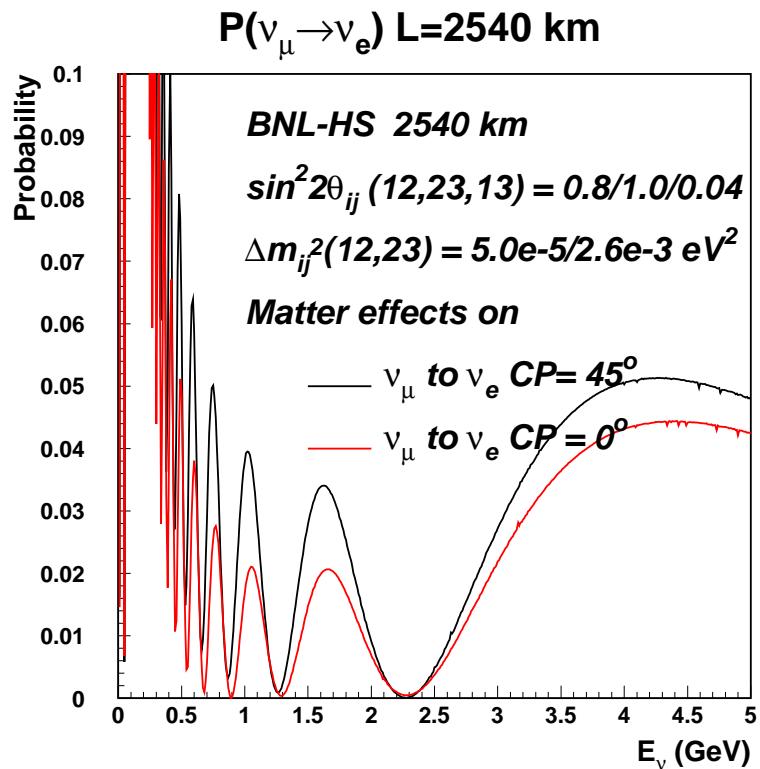
# Scaling Laws for CP Measurement

Effect of  $\delta_{CP}$  compared to first term in appearance.

$R_{CP} \equiv$  Second term divided by First Term.

$$R_{CP} \propto \sin \delta_{CP} \frac{\Delta m_{21}^2 L}{4E} \frac{1}{\sin 2\theta_{13}}$$

- $R_{CP} \propto 1/E$ . Matter effect only at high  $E$ .  
Allows separation of matter effect and CP effect.
- $R_{CP} \propto L$ . Event rate  $\propto 1/L^2$ .  
Statistical merit indep. of  $L$  for same sized detector.
- $R_{CP} \propto 1/\sin 2\theta_{13}$ . Electron event rate  $\propto \sin^2 2\theta_{13}$ .  
Statistical merit indep. of  $\theta_{13}$ .
- $R_{CP} \propto \Delta m_{21}^2$ . Better  $CP$  resolution for higher  $\Delta m_{21}^2$ .
- For given resolution on  $\delta_{CP}$  detector size is independent of L.

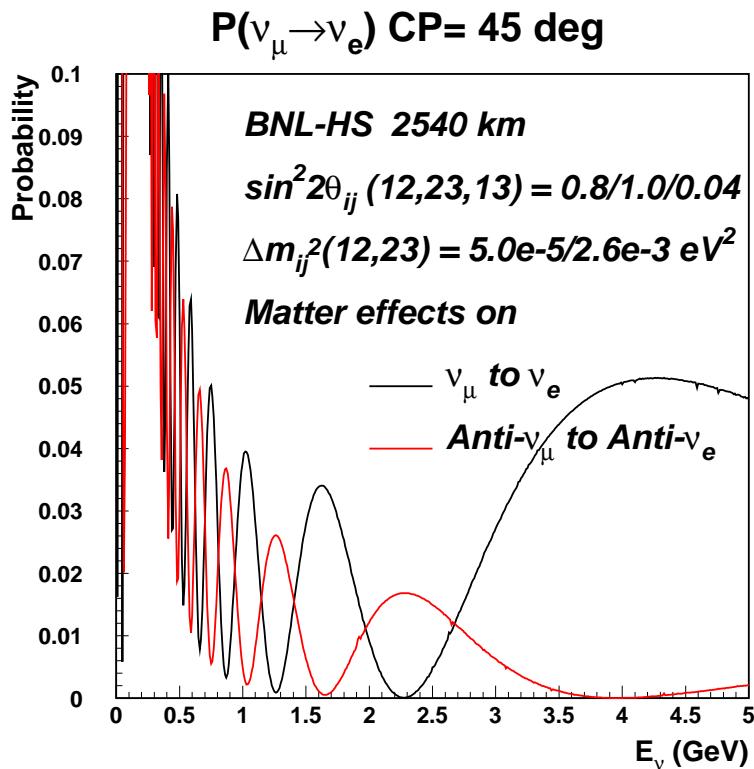


## General Features

- 0.5 – 1 GeV:  $\Delta m_{12}^2$  (LMA) region.
- 1 – 3 GeV: CP large effects region
- $> 3$  GeV: Matter enhanced ( $\nu_\mu$ ), suppressed ( $\bar{\nu}_\mu$ ). ( $\Delta m_{32}^2 > 0$ ) Region.

Exact numerical calculation

e.g. I. Mocioiu and R. Shrock, Phys. Rev. D62, 053017 (2000),  
JHEP 0111, 050 (2001)



Compare Neutrino to Antineu.

- 0.5 – 1 GeV:  $\Delta m_{12}^2$  (LMA) region.
- 1 – 3 GeV: CP region
- $> 3$  GeV: Matter enhanced ( $\nu_\mu$ ), suppressed ( $\bar{\nu}_\mu$ ). ( $\Delta m_{32}^2 > 0$ ) Region.

## 4 GOALS OF NEUTRINO OSCILLATION PHYSICS

- Precise determination of  $\Delta m_{32}^2$  and  $\sin^2 2\theta_{23}$  and definitive observation of oscillatory behavior.
- Detection of  $\nu_\mu \rightarrow \nu_e$  in the appearance mode. If  $\Delta m_{\nu_\mu \rightarrow \nu_e}^2 = \Delta m_{32}^2$  then  $|U_{e3}|^2 (= \sin^2 \theta_{13})$  is non-zero.
- Detection of the matter enhancement effect in  $\nu_\mu \rightarrow \nu_e$ . Sign of  $\Delta m_{32}^2$ ; i.e. which neutrino is heavier.
- Detection of CP violation in neutrino physics. Phase of  $|U_{e3}|$  is CP violating and causes asymmetry in the rates  $\nu_\mu \rightarrow \nu_e$  versus  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ .

It will be good to do it all in same experiment with only neutrino beam (no antineutrino).

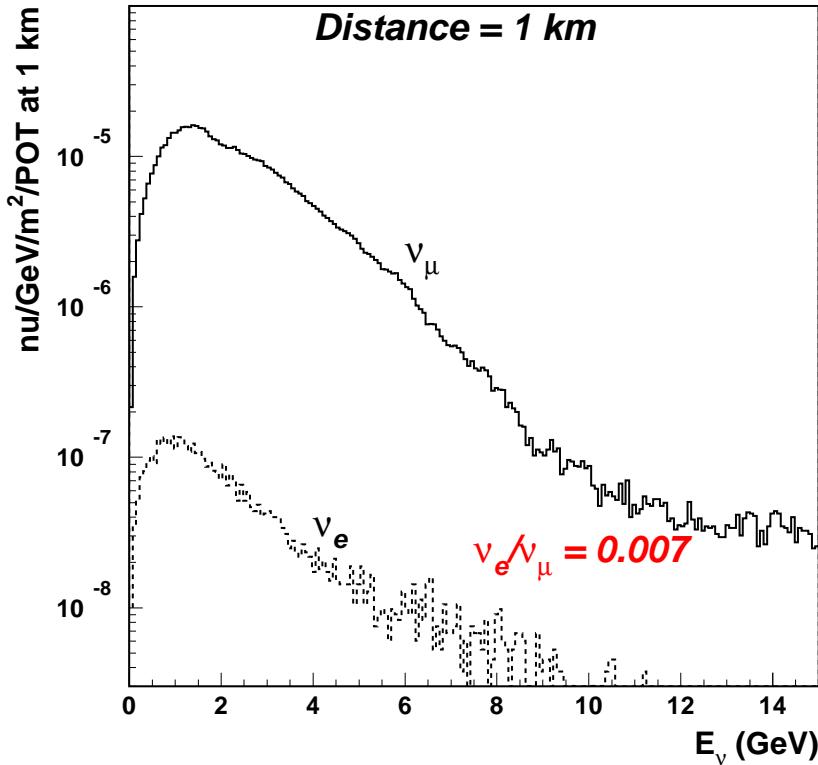
## Summary of our study

- Baseline of  $> 2000$  km with wide band conventional beams are the next step in accelerator neutrino physics.
- Extraordinary, large physical effects will be seen in such an experiment.
- Very good sensitivity to neutrino properties.
  - $< 1\%$  resolution on  $\Delta m_{32}^2$
  - $< 1\%$  resolution on  $\sin^2 2\theta_{23}$
  - Sensitivity to  $\sin^2 2\theta_{13} > 0.005$  over a wide range of  $\Delta m_{32}^2$
  - Sensitivity to CP violation.
  - Sign of  $\Delta m_{32}^2$  over a wide range of parameters.
  - Measurement of  $\Delta m_{21}^2$  in LMA region.
- Requires new thinking on how to build a beam and a detector. But experiment is technically feasible.

## Comments

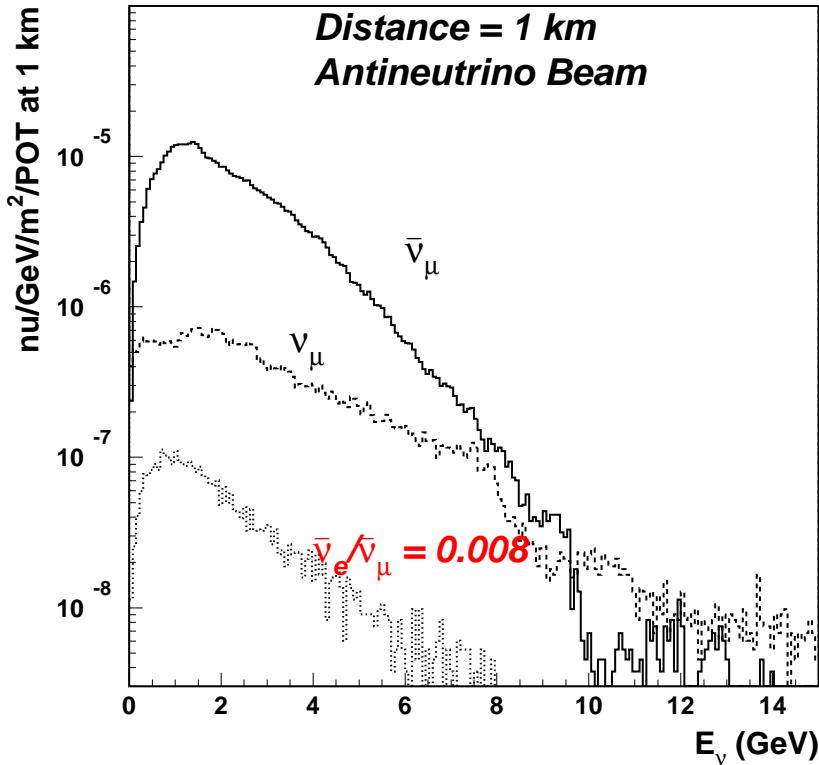
- Important ideas here are:
  - Long baseline to achieve large effects
  - Low energy wide band beam to get spectra
  - Beam is wide band, but low energy to make low backgrounds to  $\nu_e$  appearance signature.
- Important difference between quark-matrix and neutrino-matrix
  - Neutrino oscillation effects are exactly calculable for any given set of parameters.  
(including matter)
  - For quarks we often need complex tools such as CHPT and Lattice to connect CKM-matrix to physical phenomena.
- It makes sense to make a neutrino oscillation experiment with large effects even if they are sensitive to multiple parameters.

## BNL Wide Band. Proton Energy = 28 GeV



- New design spans 0.5-6 GeV
- Low  $\nu_e$  background 0.7%  
 $0.0073 \pm 0.0014$  (E734 1986).
- Low background from high energies (NC and  $\nu_\tau$  for  $\nu_e$ )
- 200 m decay tunnel
- Graphite target embedded in horn
- Target cooling achievable for 1 MW

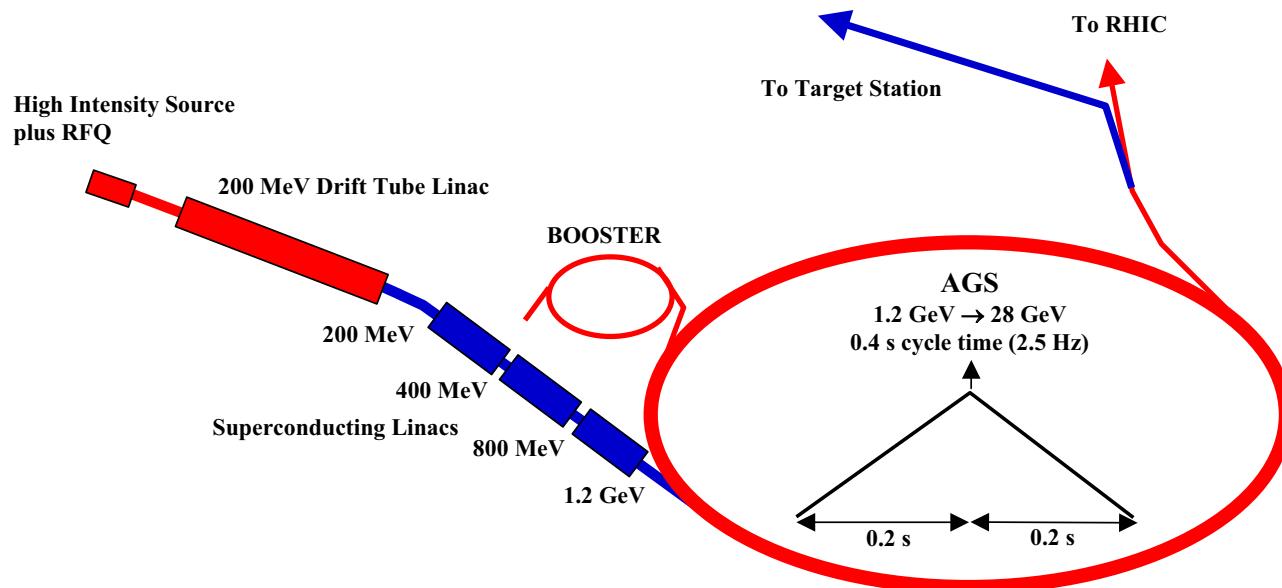
## BNL Wide Band. Proton Energy = 28 GeV



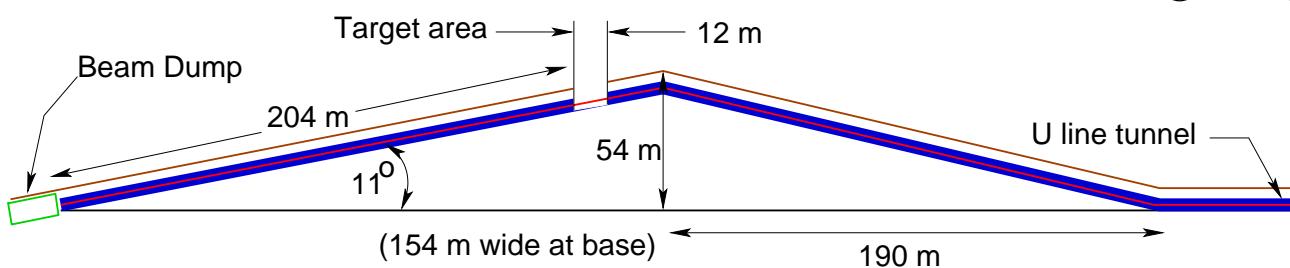
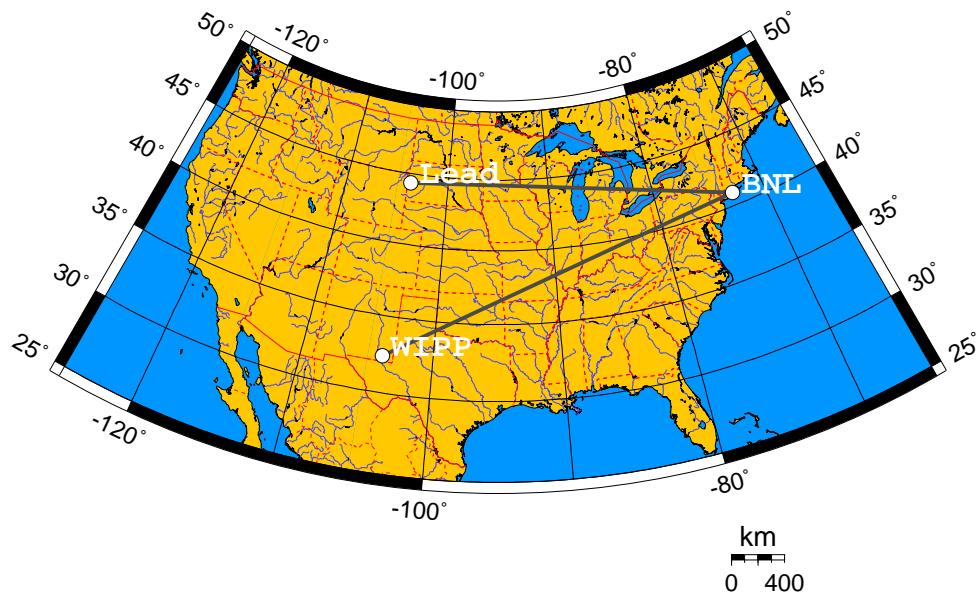
- Antineutrino beam has larger neutrino contamination.
- Will need to go to 2 MW to get statistics equal to neutrino.

# The Accelerator

- Conceptually simple upgrade. No magic.
- Run 28 GeV AGS at 2.5 Hz to get 1 MW.
- Need faster proton source: Super Conducting LINAC at 1.2 GeV
- Current:  $7 \times 10^{13} ppp$  at 0.5 Hz => LINAC:  $10^{14} ppp$  at 2.5 Hz.



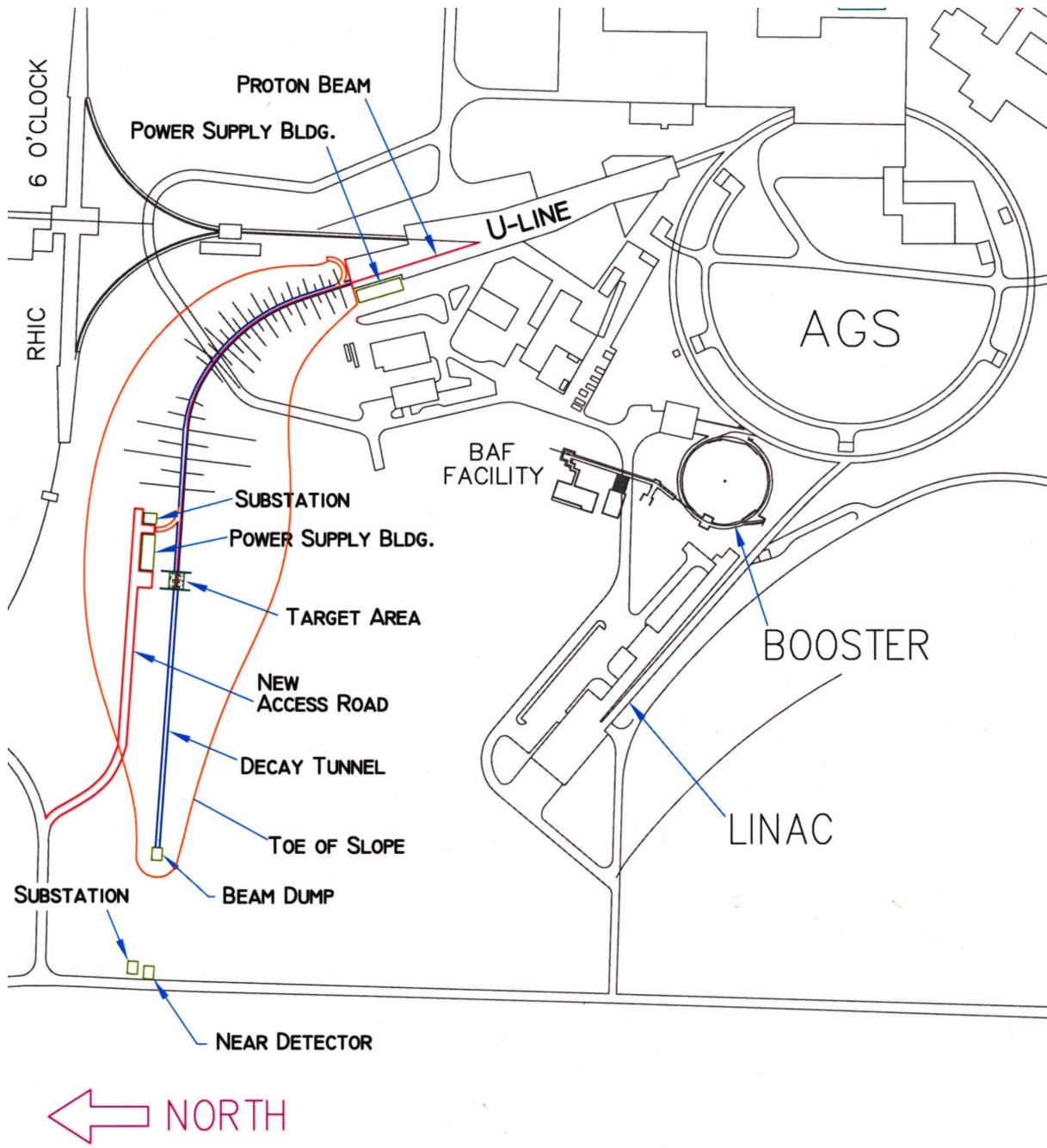
# Beam on the Hill



- BNL-Lead 2540km  
BNL-Wipp: 2880km
- Avoids water table.
- Hills are inexpensive:  
highway ramps.

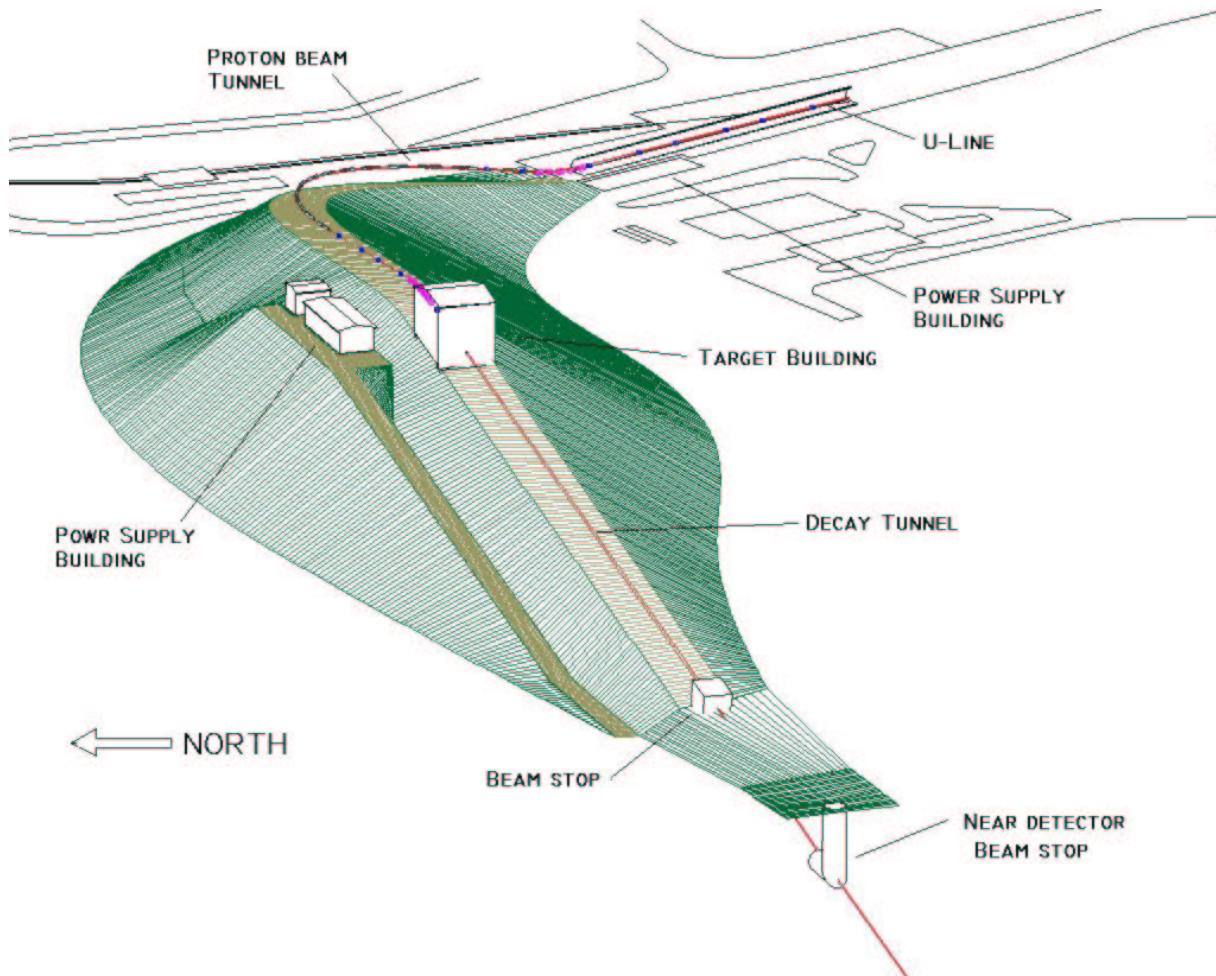
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# Beam Layout

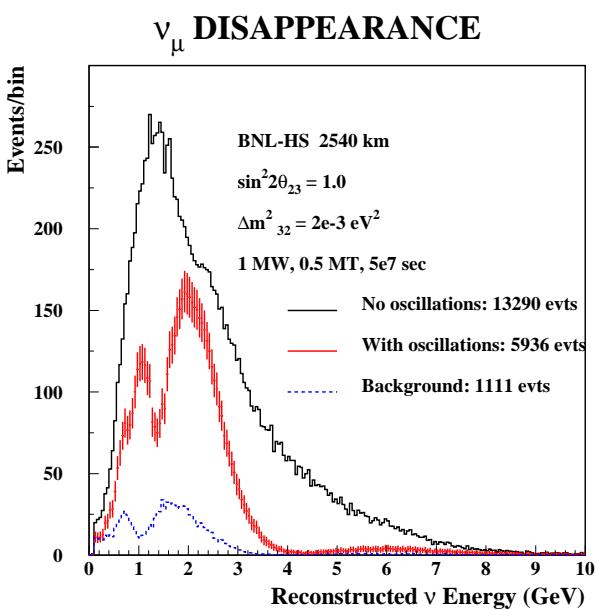
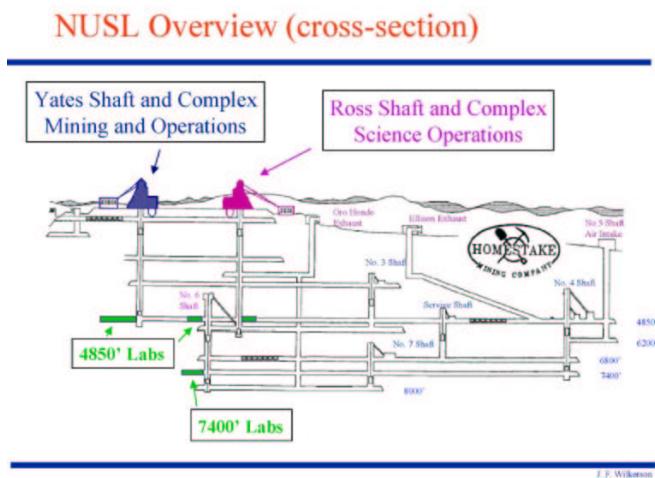
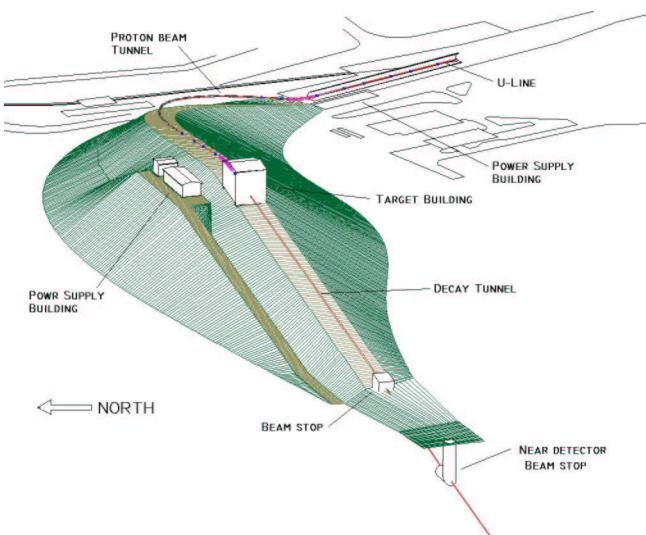
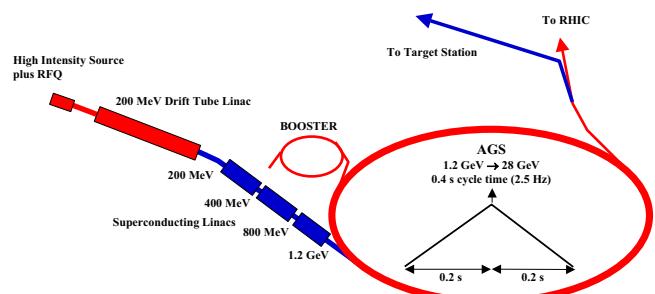


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## Beam 3d



# 1 MW beam - 2540 km - 500 kT detector



## Event Rates with Neutrinos

Assume 1 MW, 500 kT Fiducial,  $5 \times 10^7$  sec running. ( $1.22 \times 10^{22}$  Protons at 28 GeV.)

Assume Water Cerenkov detector.

CC $\nu_\mu + N \rightarrow \mu^- + X$	51800 (15160)
NC $\nu_\mu + N \rightarrow \nu_\mu + X$	16908 (5770)
CC $\nu_e + N \rightarrow e^- + X$	380 (103)
QE $\nu_\mu + n \rightarrow \mu^- + p$	11767 (5934)
QE $\nu_e + n \rightarrow e^- + p$	84 (40)
CC $\nu_\mu + N \rightarrow \mu^- + \pi^+ + N$	14574 (4200)
NC $\nu_\mu + N \rightarrow \nu_\mu + N + \pi^0$	3178 (1156)
NC $\nu_\mu + O^{16} \rightarrow \nu_\mu + O^{16} + \pi^0$	574 (202)
CC $\nu_\tau + N \rightarrow \tau^- + X$ (depends on $\Delta m^2$ )	$\sim 110$ (20)

Backgrounds to clean (QE) events SMALL

NC dominated by elastic and single  $\pi$ .

Low  $\tau$  production.

Anti-neutrino rate in (brackets) for 1 MW. Neutrino contamination additional.

## Neutral Current Events Neutrinos

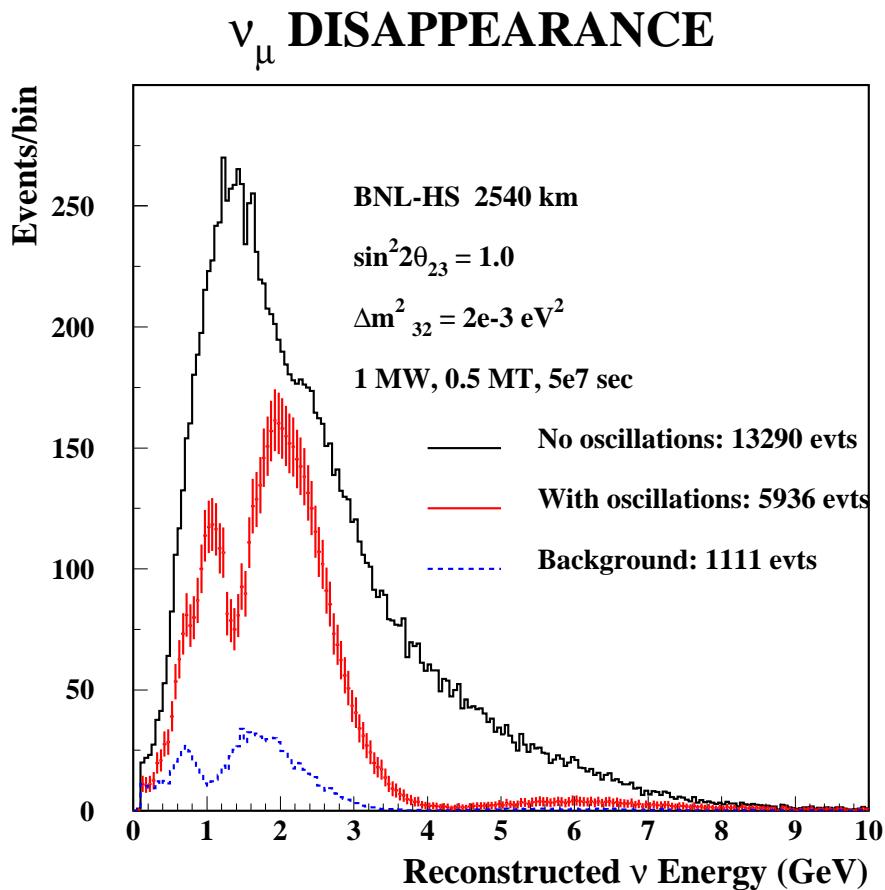
Assume 1 MW, 500 kT Fiducial,  $5 \times 10^7$  sec running. ( $1.22 \times 10^{22}$  Protons at 28 GeV.)

Assume Water Cerenkov detector (with  $\sim 10\%$  PMT coverage)

NC $\nu_\mu + N \rightarrow \nu_\mu + X$	16908
Single $\pi^0$	3700
Single $\pi^\pm$	3500
$\nu + n \rightarrow \nu + n$	2000
$\nu + p \rightarrow \nu + p$	2000
Multi-pi (0 $\pi^0$ )	2900
Multi-pi ( $\geq 1 \pi^0$ )	2900

Multiple pion events should be suppressed better than single  $\pi^0$  events.

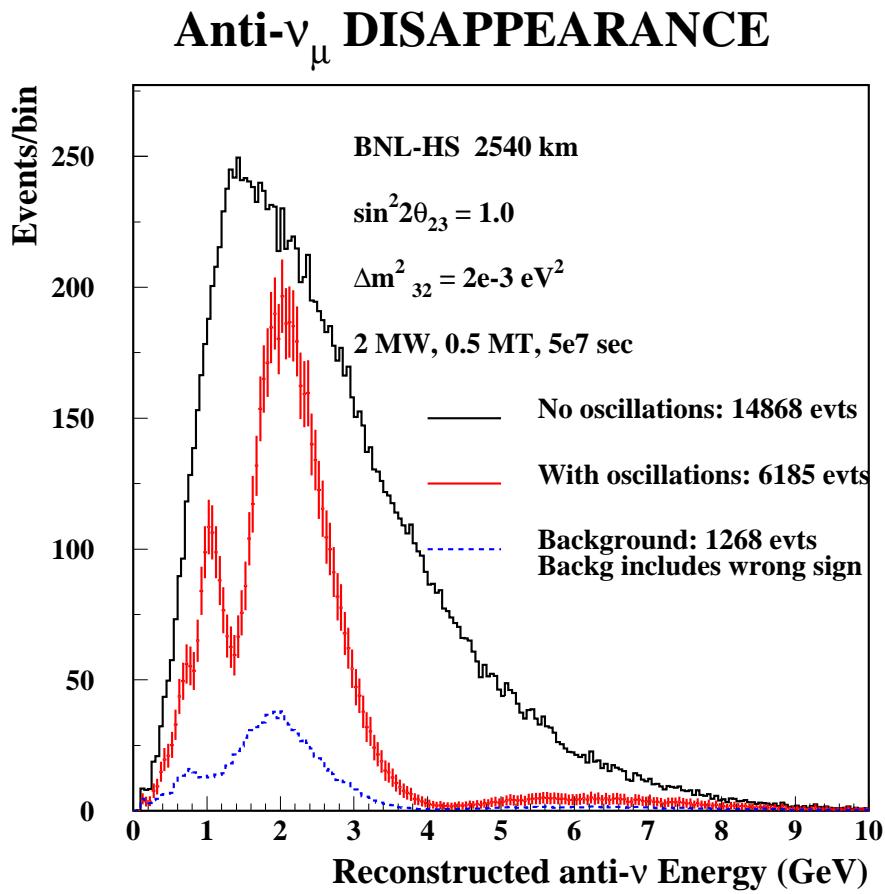
Both single and multi-pi event rate display the same tendency to fall rapidly with energy.



Node pattern provides high  $\Delta m^2_{32}$  resolution.  
 Energy calibration is very important.

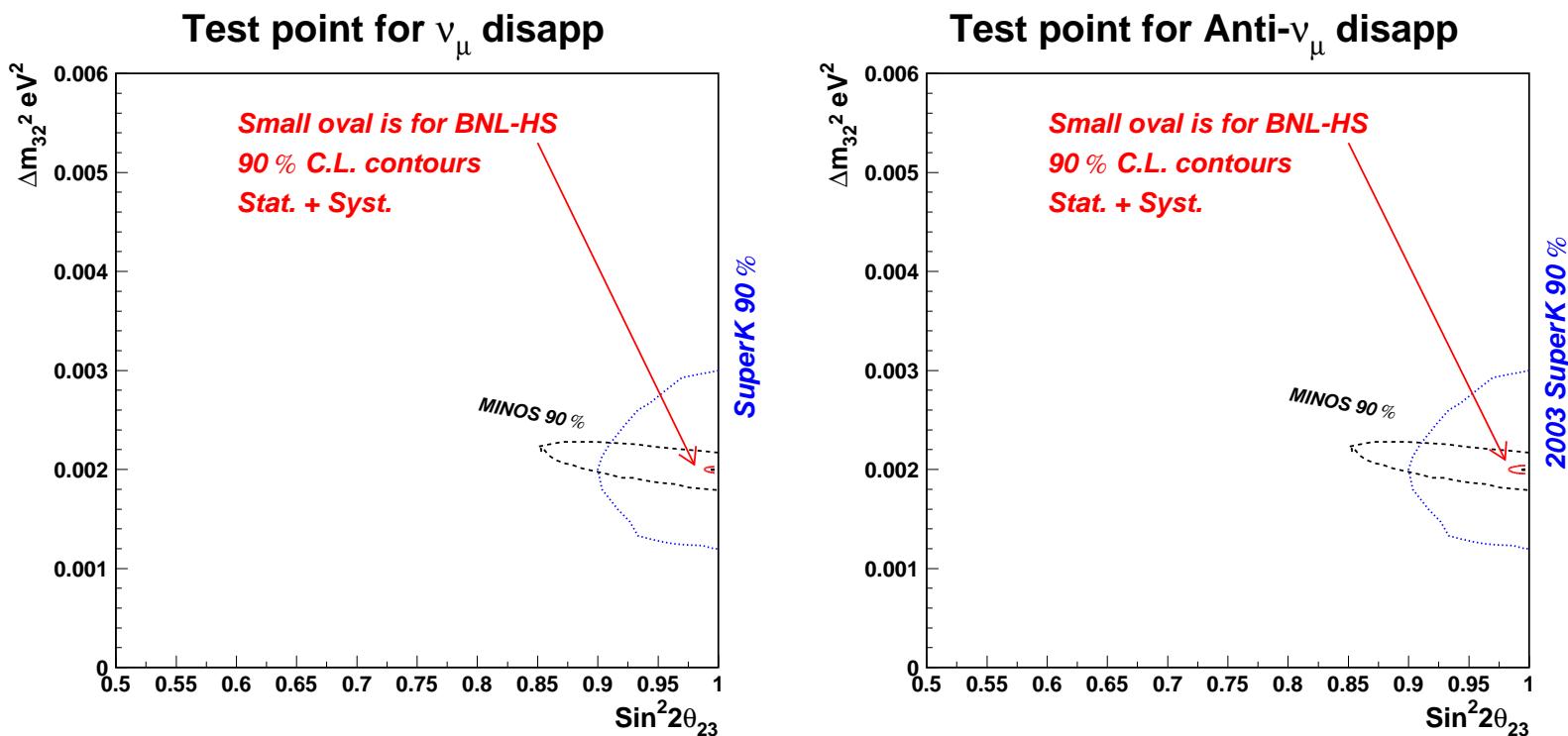
Flux normalization not important for  
 measurement of  $\sin^2 2\theta_{23}$

Background shape can be measured independently  
 Minimum systematics in  $\nu_\mu$  and  $\bar{\nu}_\mu$  comparison



For anti-neutrinos low energy nodes have less statistics because of cross section.

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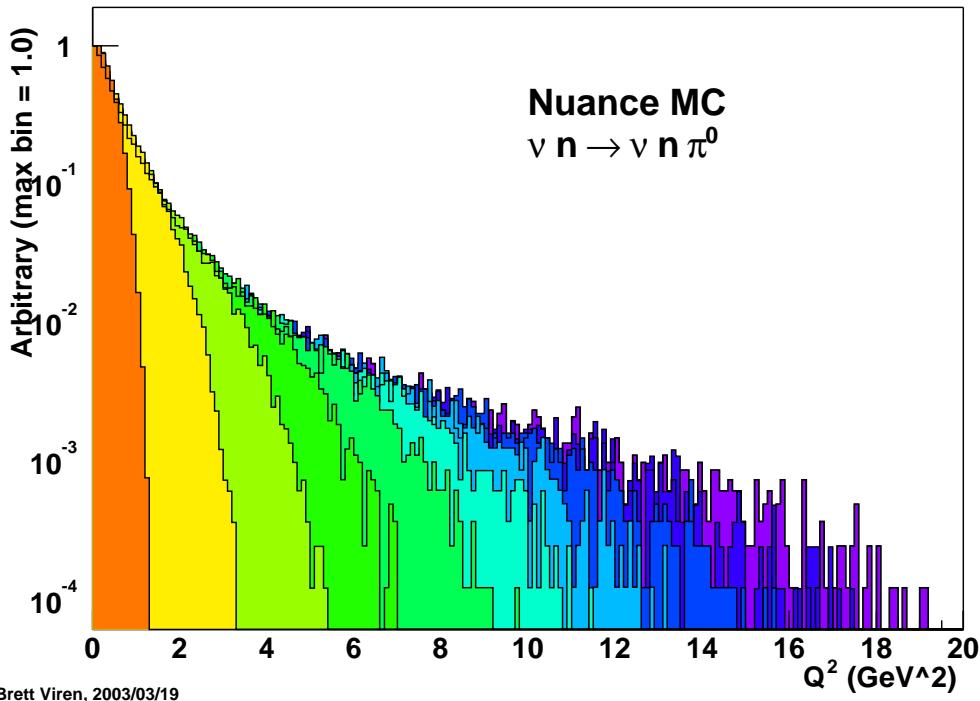


## Measurement of $\Delta m_{32}^2$

- Little dependence on systematic errors on resolution, backgrounds, energy linearity, or normalization.
- Ultimate resolution on  $\Delta m^2$  depends on energy calibration. For perfect energy calibration  $\pm 0.7\%$  possible.
- Energy calibration at  $< 1\%$  in 1-5 GeV region needed.
- Can exclude  $\sin^2 2\theta_{23} < 0.99$  at 90% C.L.  
Could be better with accurate background subtraction.
- No need of near detector for this measurement. Even a 10% systematic error on normalization does not bother measurement.
- neutrino-antineutrino comparison free of most systematics (even cross section) because of nodal pattern. Possible to measure difference in  $\Delta m_{32}^2$  of  $< 1\%$ .

# NC $\pi^0$ background for $\nu_\mu \rightarrow \nu_e$

$Q^2$  for  $E_\nu = 1\text{-}10 \text{ GeV}$



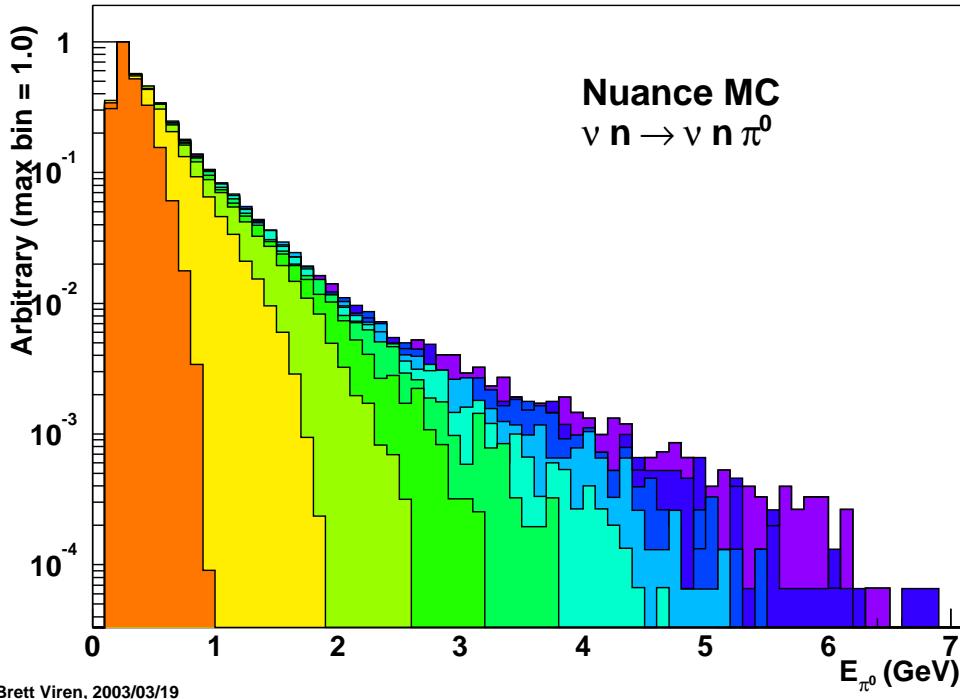
$$q^2 = (p'_N + p'_\pi) - p_N.$$

General feature of all neutral current processes:

Low  $q^2$  or low hadronic energy in final state independent of neutrino energy.

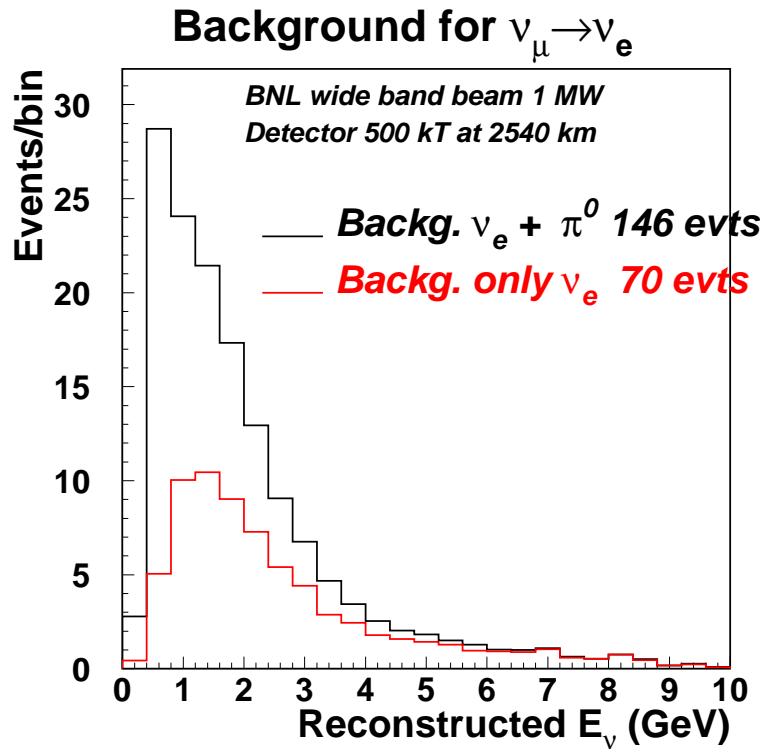
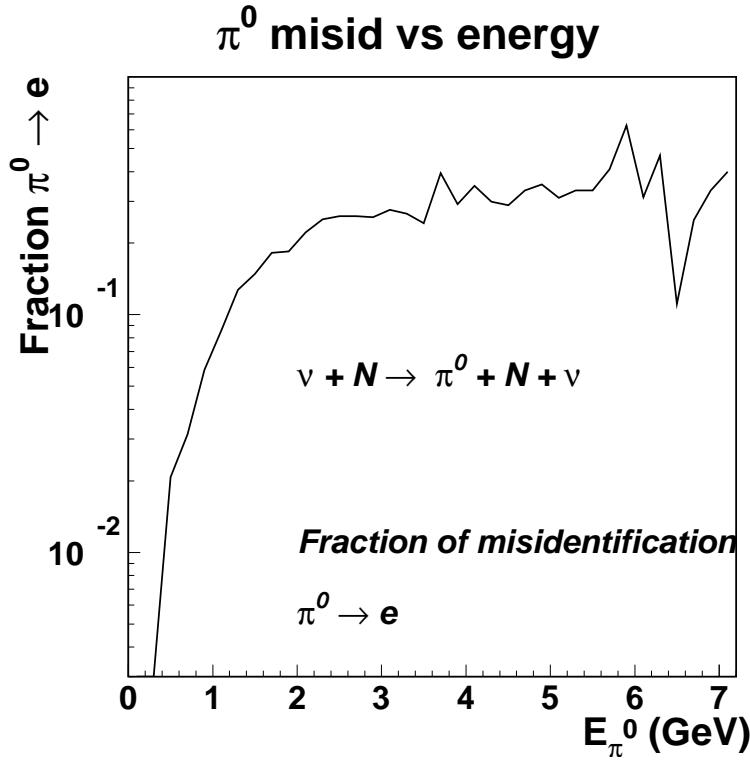
## NC $\pi^0$ background for $\nu_\mu \rightarrow \nu_e$

$E_{\pi^0}$  for  $E_\nu = 1\text{-}10 \text{ GeV}$



- The NC energy distribution is independent of  $\nu$ -energy except the kinematic limit.
- In  $\nu_\mu N \rightarrow \nu_\mu N \pi^0$  events all energy  $\nu$  produce peak at the same energy except the tail.
- For a very long baselines and wide band beam  $\nu_e$  signal will be above 3 GeV with little  $\pi^0$  background.

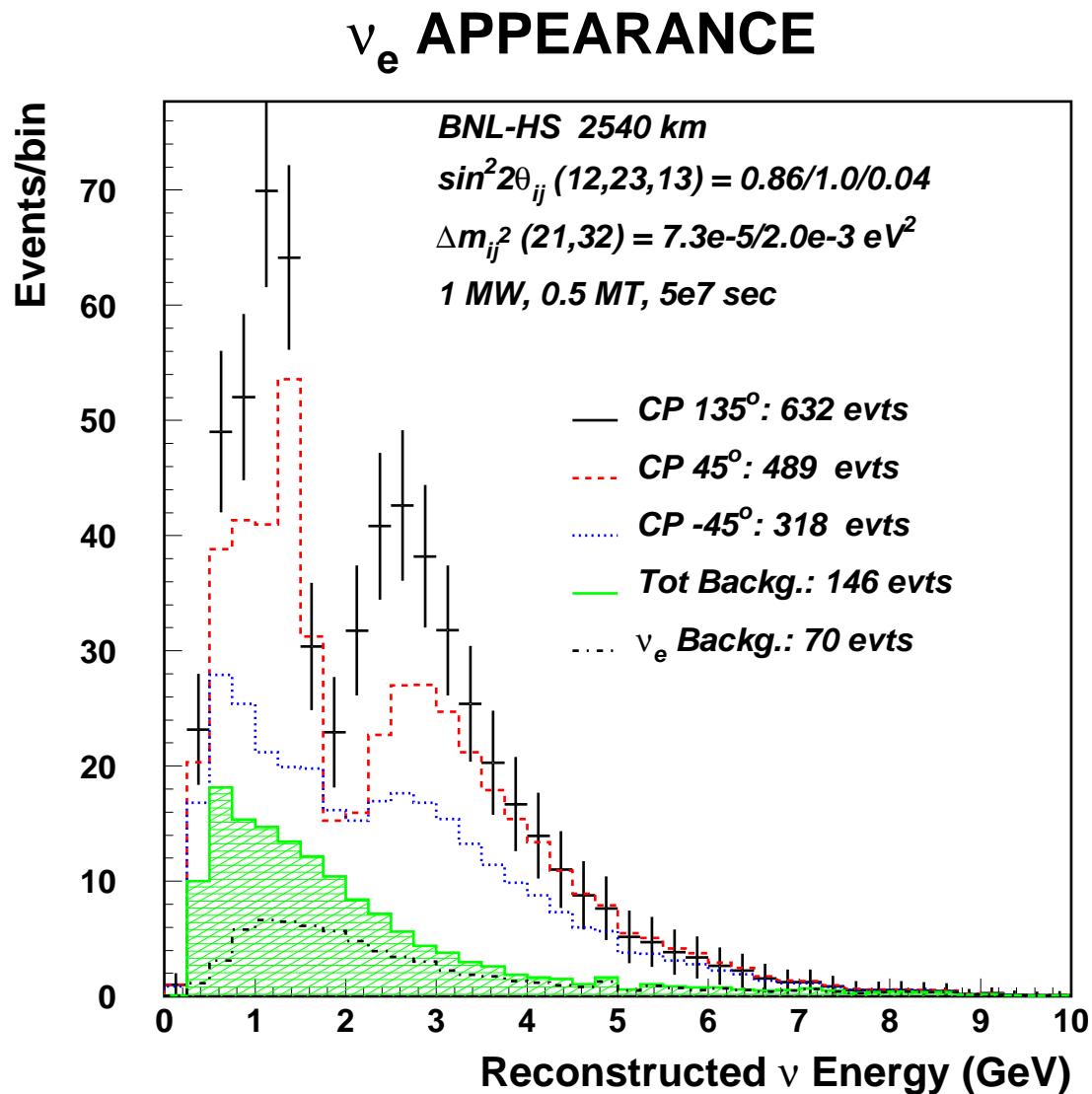
# $\nu_\mu \rightarrow \nu_e$ All background



- Background includes  $\nu N \pi^0$  and Coherent  $\nu O^{16} \pi^0$ .
- Efficiency for signal is  $\sim 80\%$
- For  $E_\nu < 2\text{GeV}$   $N_{\pi^0} : N_{\nu_e} :: 59 : 35$
- For  $E_\nu > 2\text{GeV}$   $N_{\pi^0} : N_{\nu_e} :: 17 : 35$

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# Measurement of $\sin^2 2\theta_{13}$

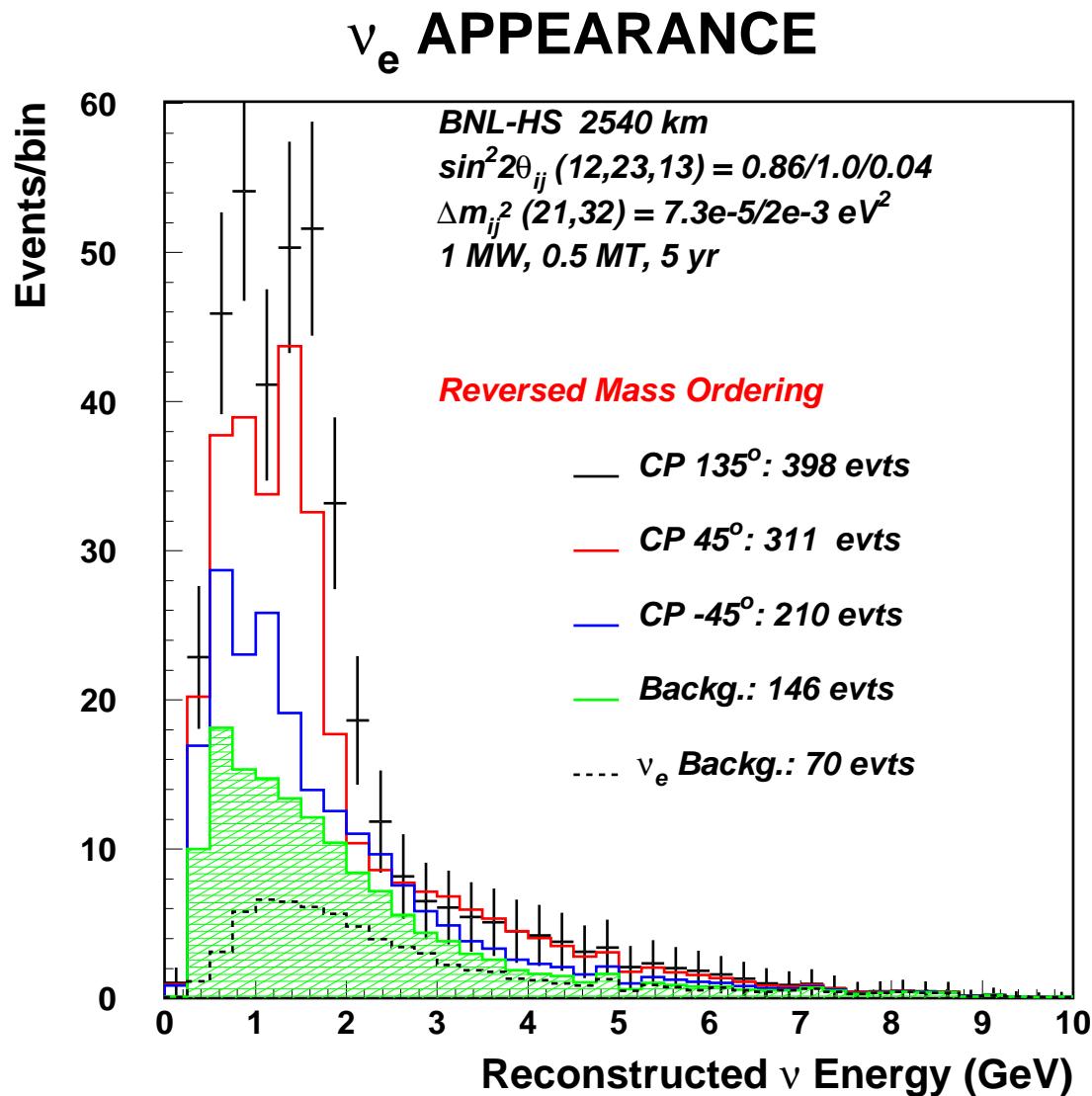


$$\Delta m_{32}^2 = 0.002 \text{ eV}^2, \sin^2 2\theta_{13} = 0.04.$$

Assume normal mass hierarchy.  $m_3 > m_2 > m_1$

Matter effects included.

# Measurement of $\sin^2 2\theta_{13}$

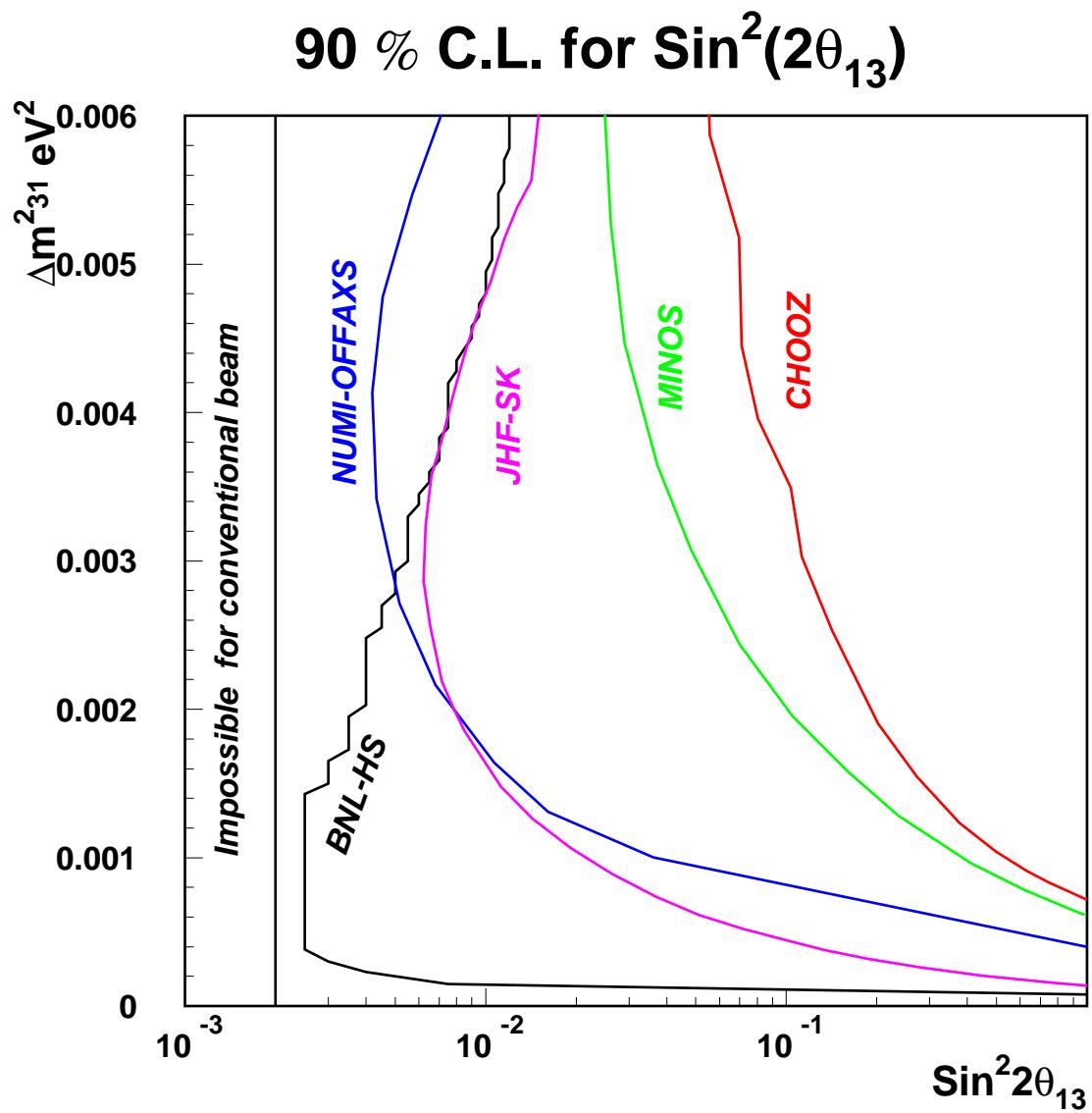


$$\Delta m_{32}^2 = 0.002 \text{ eV}^2, \sin^2 2\theta_{13} = 0.04.$$

Reversed Mass Hierarchy

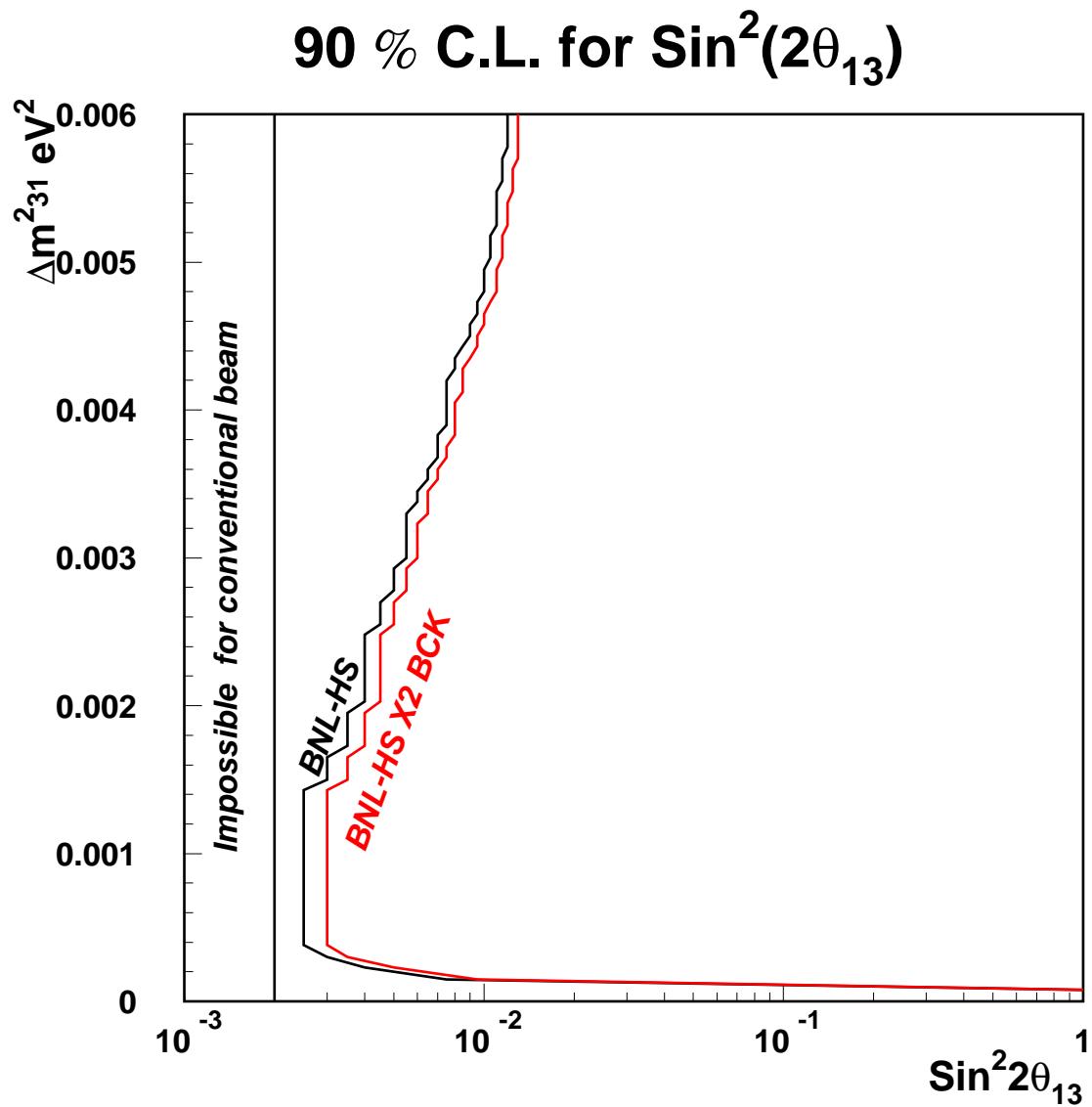
Matter effects included.

# Measurement of $\sin^2 2\theta_{13}$ 90% C.L.



Distinctive signature with multiple oscillations  
above  $0.001 \text{ eV}^2$

# Measurement of $\sin^2 2\theta_{13}$ 90% C.L. high Bckg.



Assume that the neutral current background is higher by factor of 2 over the entire spectrum.

## Measurement of $\sin^2 2\theta_{13}$ 90% C.L.

BNL-HS(2540 km) good sensitivity to  $\sin^2 2\theta_{13}$ .

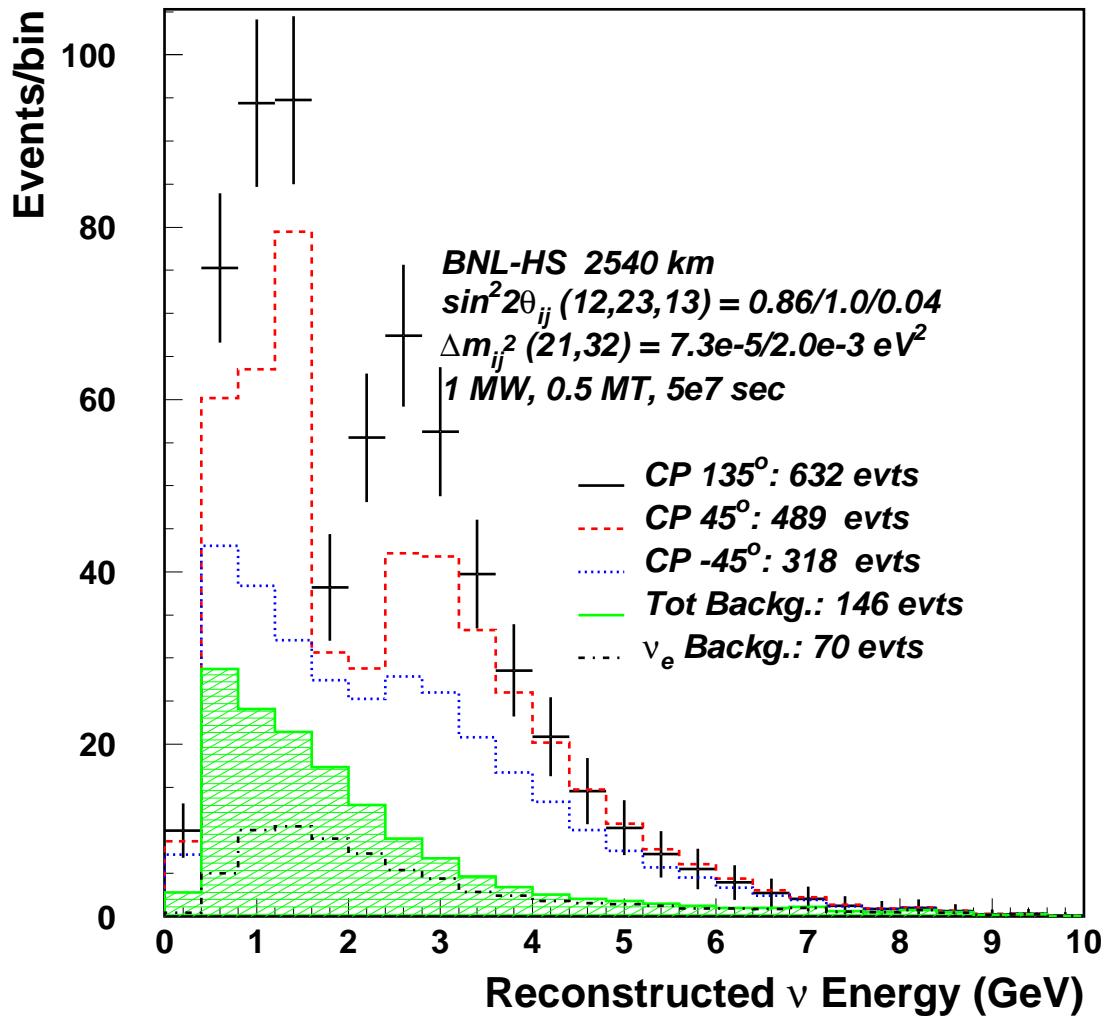
Improvement from 0.12 to 0.005 at  $0.0025 \text{ eV}^2$ .

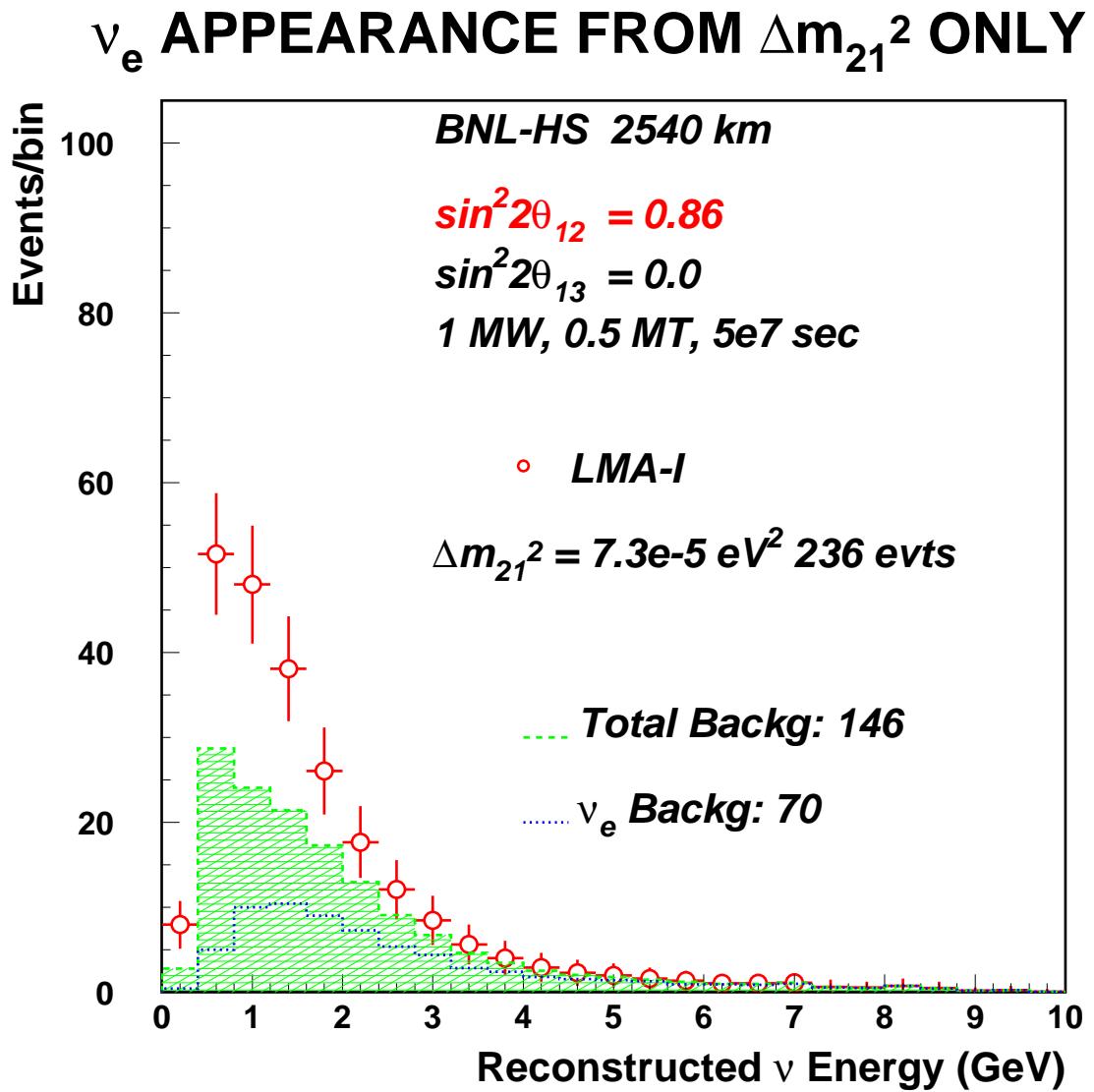
Signal very distinctive above  $0.001 \text{ eV}^2$ .

Need harder beam to improve sensitivity above  $0.004 \text{ eV}^2$ .

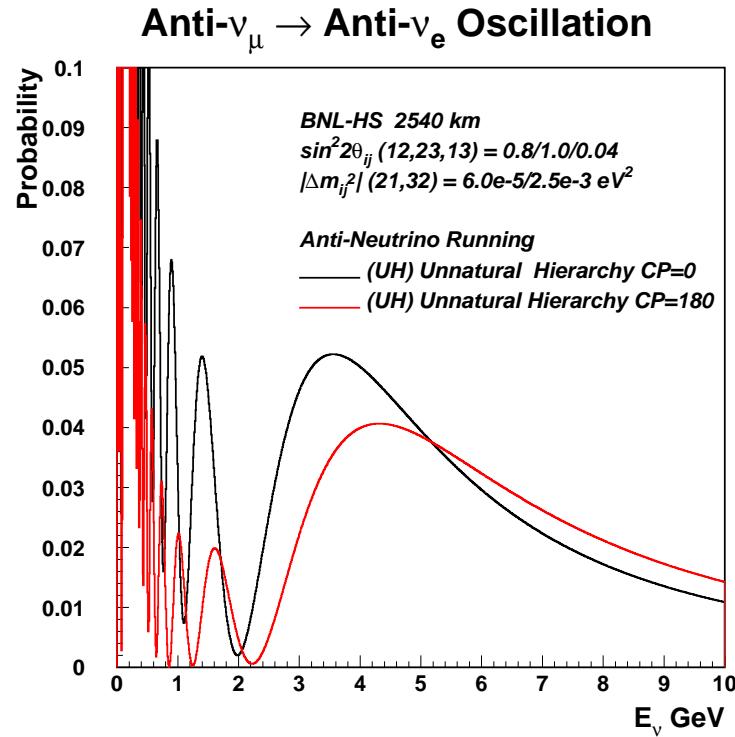
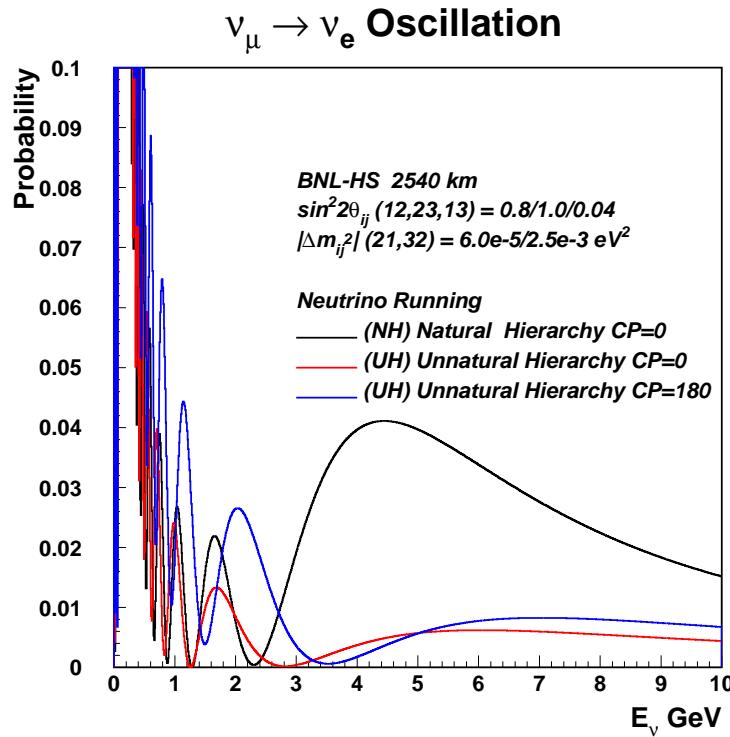
No experiment can go below  $\sin^2 2\theta_{13} \approx 0.002$  with horn focussed beam due to systematic error on intrinsic  $\nu_e$  background.

## $\nu_e$ APPEARANCE



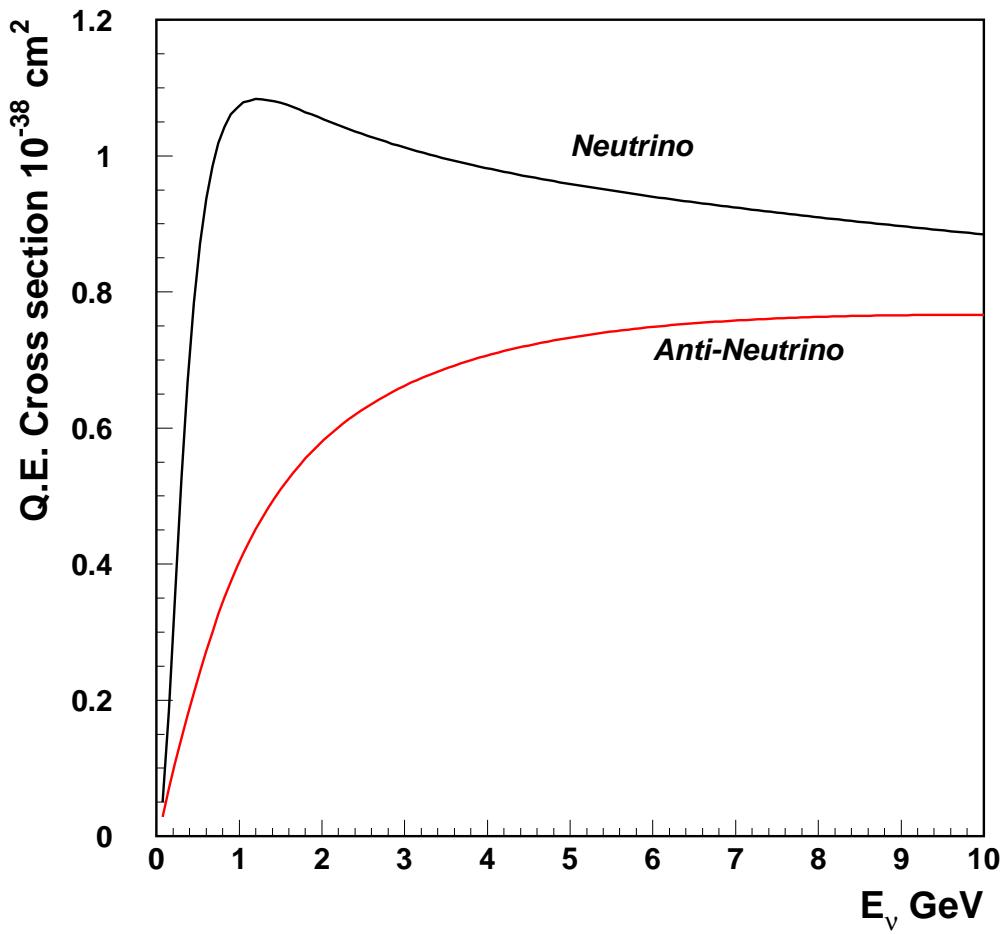


# Mass Hierarchy Anti-neutrinos



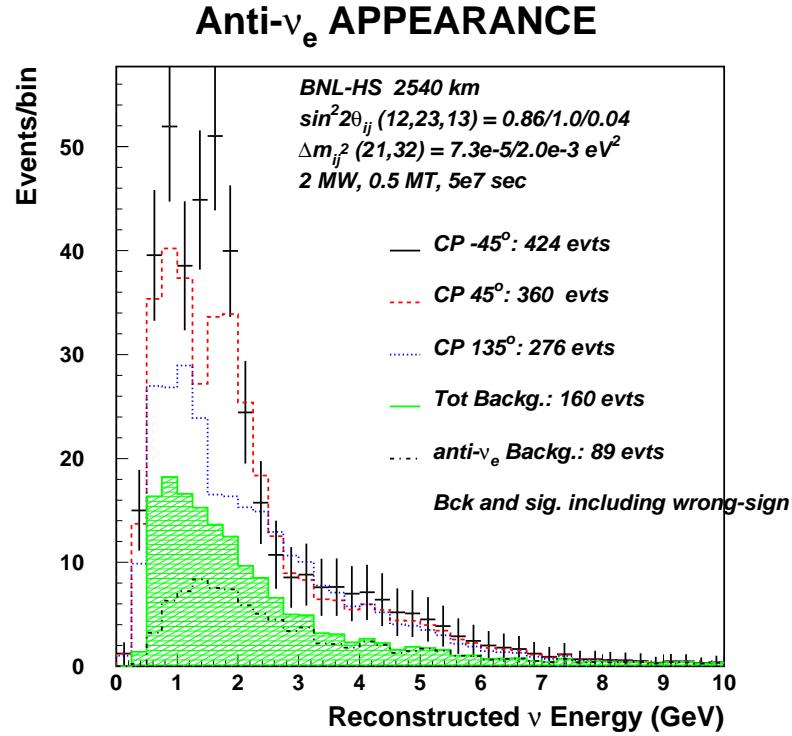
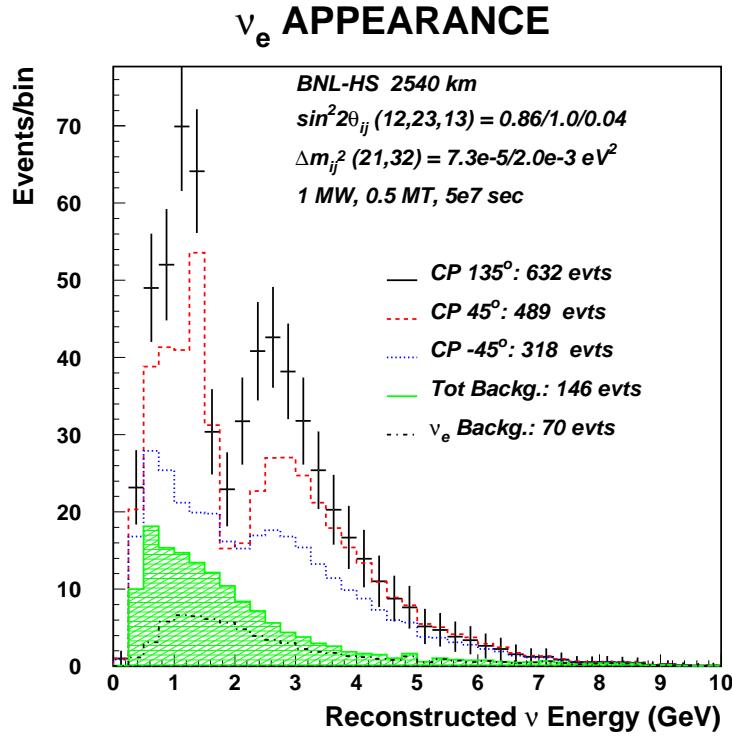
Very long baselines with a superbeam

## Quasielastic cross section



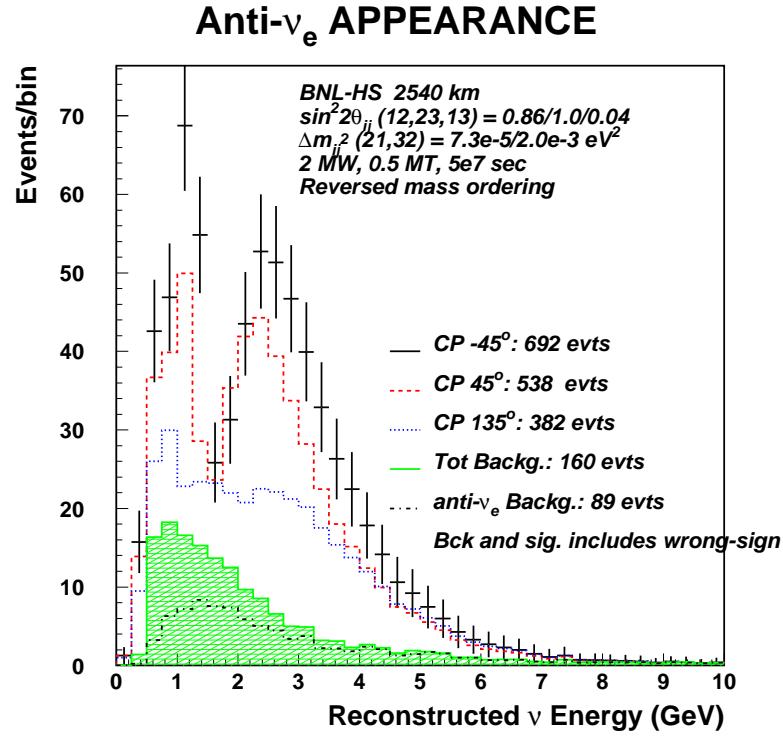
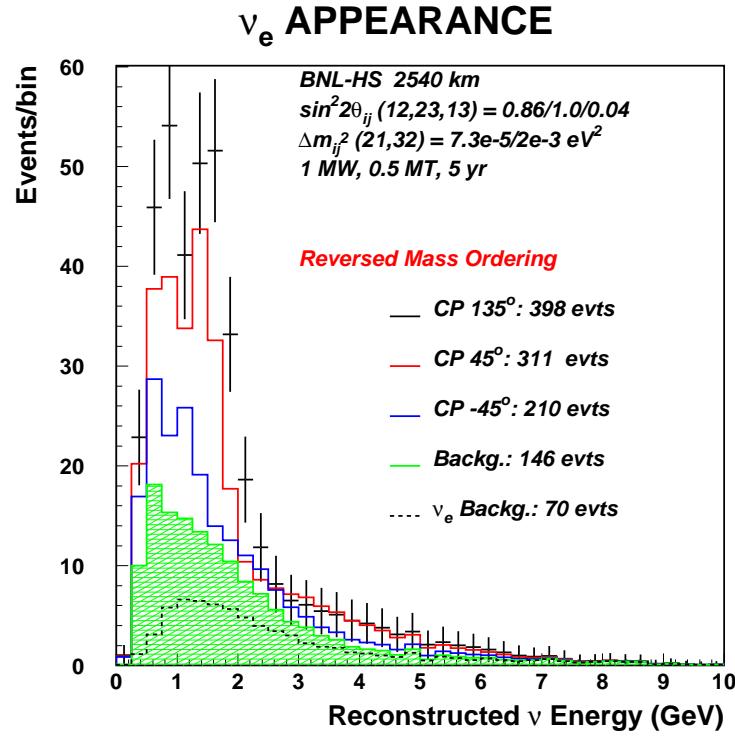
An experiment searching for signal at high energies may not need much more anti-neutrino running than neutrino running.

# Running for $\sin^2 2\theta_{13}$



$\Delta m_{32}^2 = 0.002 \text{ eV}^2$ ,  $\sin^2 2\theta_{13} = 0.04$ . Assume normal mass hierarchy.  $m_3 > m_2 > m_1$  Matter effects included.

# Running for $\sin^2 2\theta_{13}$



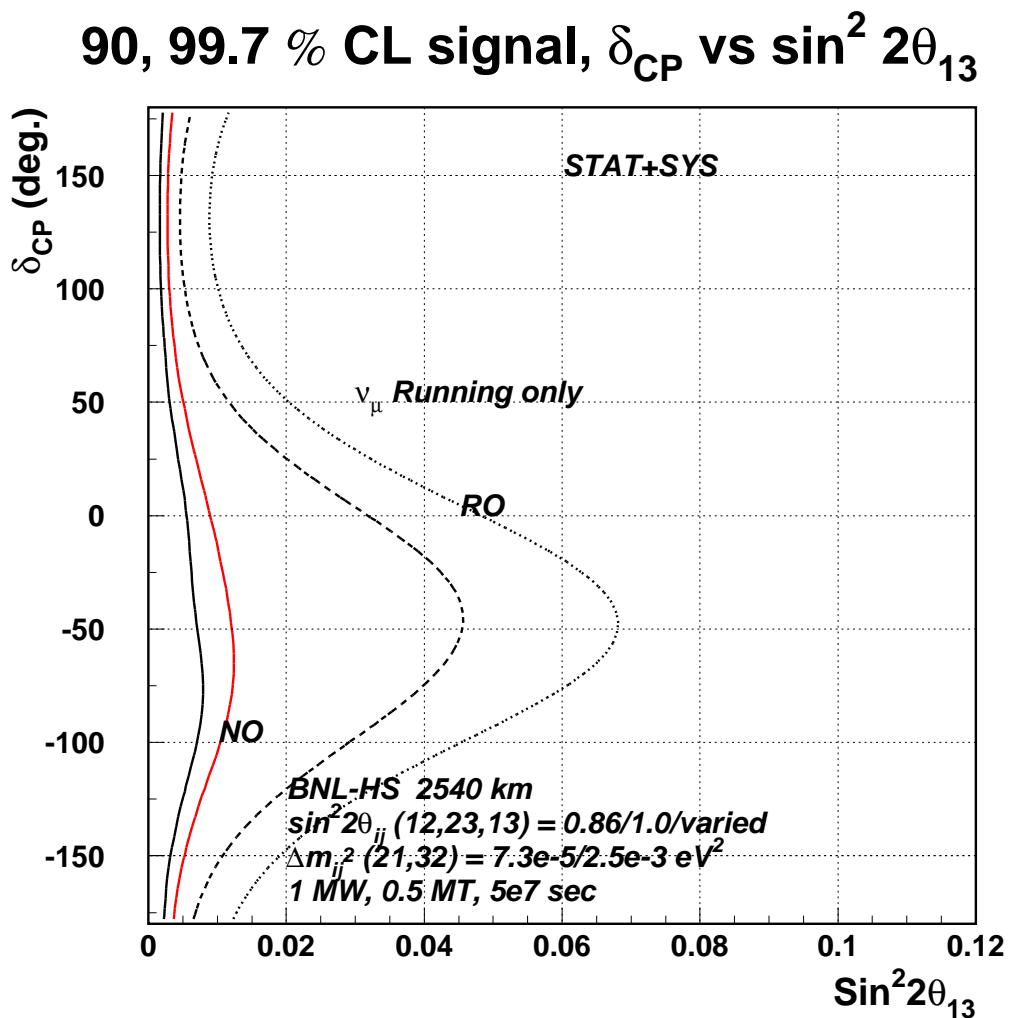
$$\Delta m_{32}^2 = 0.002 \text{ eV}^2, \sin^2 2\theta_{13} = 0.04.$$

Reversed Mass Hierarchy

Matter effects included.

Very long baselines with a superbeam

## Mass Hierarchy



Natural Mass hierarchy:  $m_3 > m_2 > m_1$  (NO)

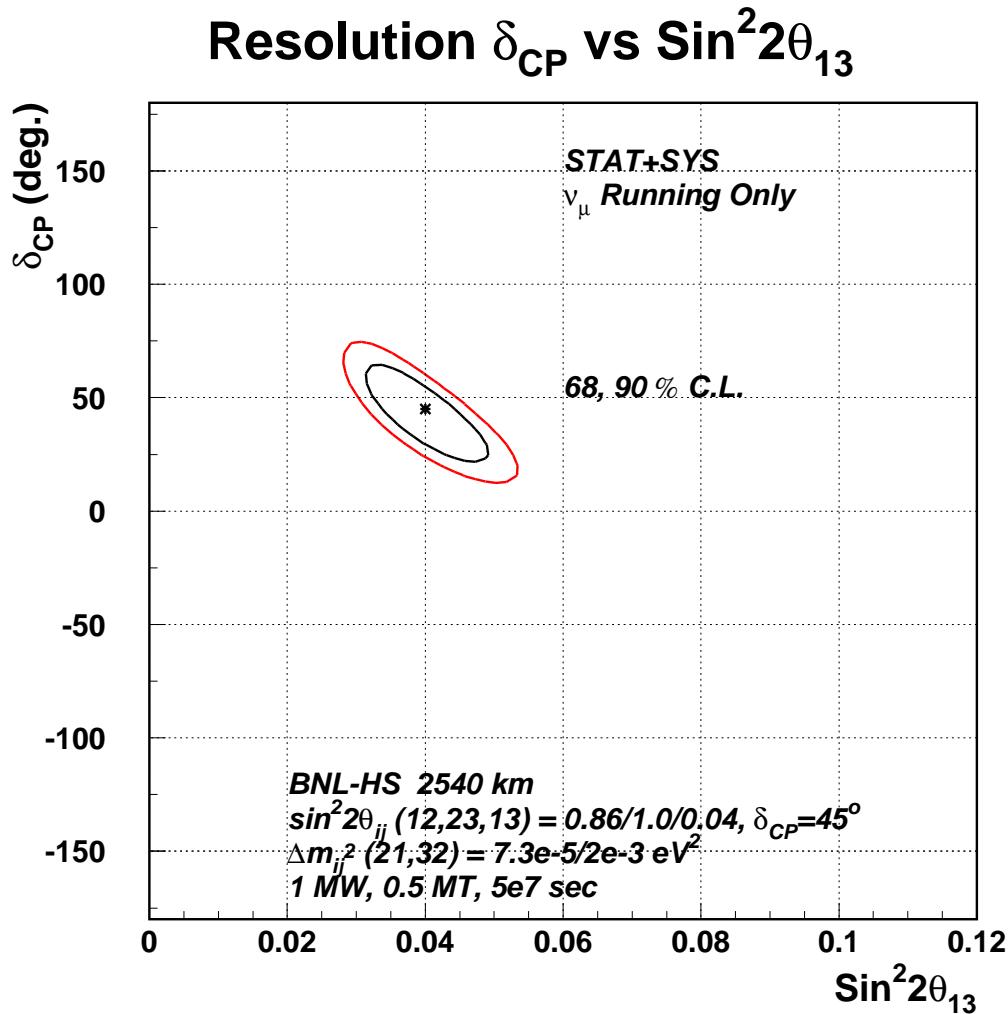
Reversed Mass hierarchy:  $m_1 > m_2 > m_3$  (RO)

Unnatural Mass hierarchy:  $m_2 > m_1 > m_3$  (RO)

$m_1 > m_2$  is ruled out if Solar LMA is the correct solution.

We would need to run Anti-neutrino beam to fully explore RO.

**Measurement of  $\delta_{CP} = 45^\circ$**   
**No anti-neutrino running.**



Systematic error of 10% on backg.

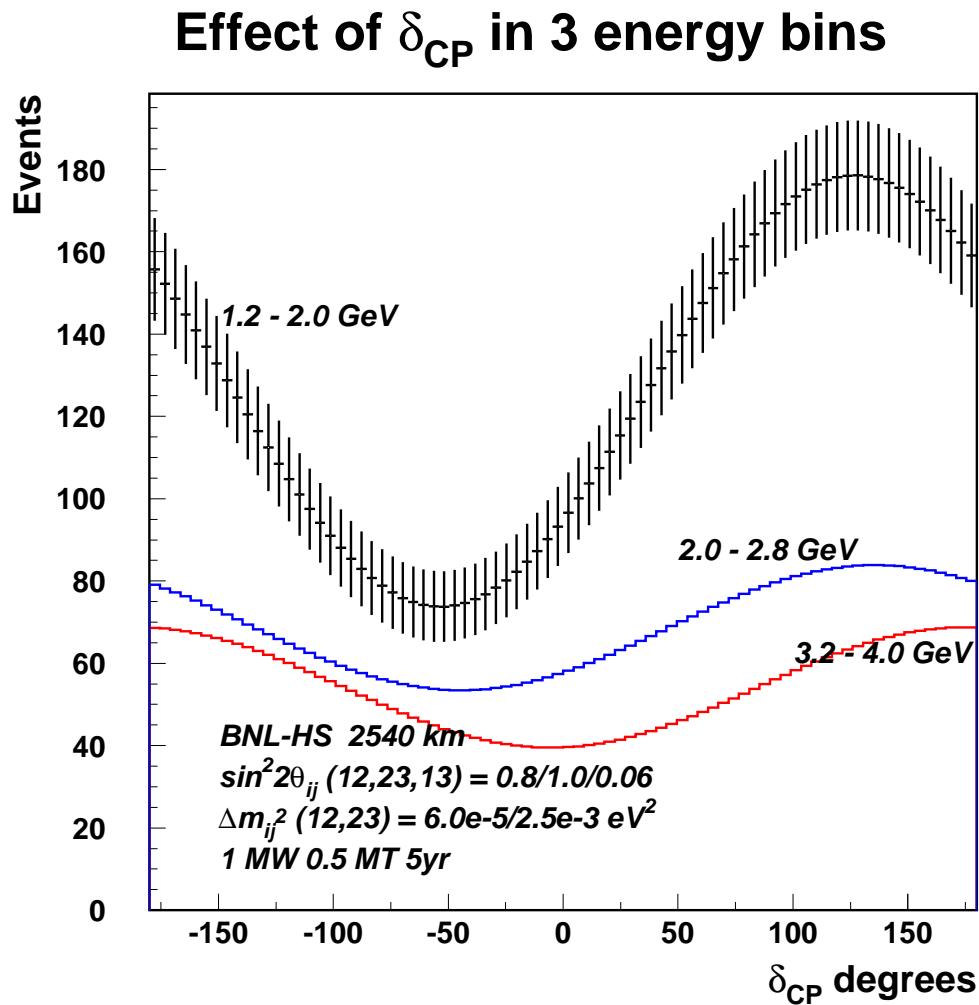
$$\Delta m_{21}^2 = 7.3 \times 10^{-5} \text{ eV}^2, \Delta m_{31}^2 = 2 \times 10^{-3} \text{ eV}^2$$

$$\sin^2 2\theta_{12} = 0.86, \sin^2 2\theta_{23} = 1.0$$

$$\delta_{CP} = 45^\circ, \sin^2 2\theta_{13} = 0.04$$

68%, and 90% C.L.

## Effect of $\delta_{CP}$ on the spectrum.



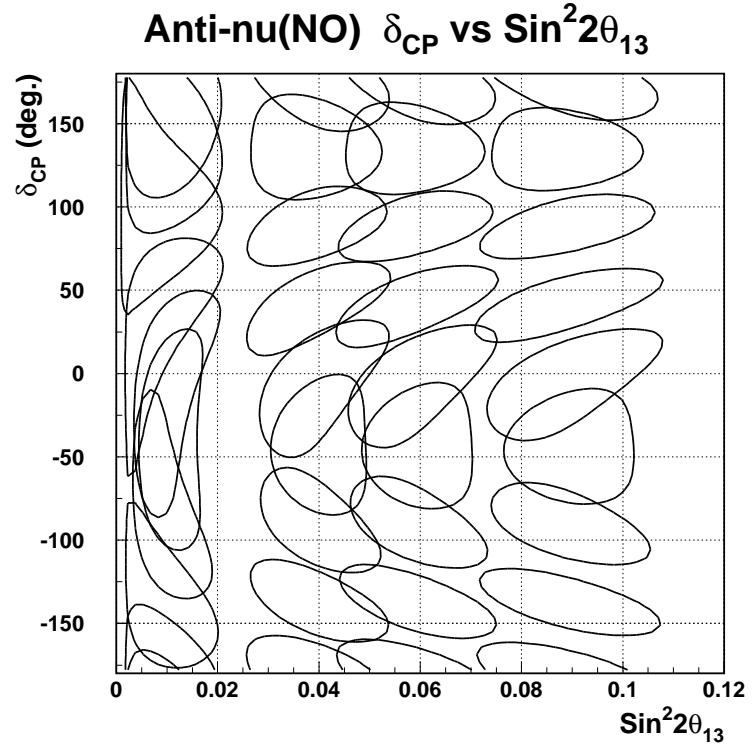
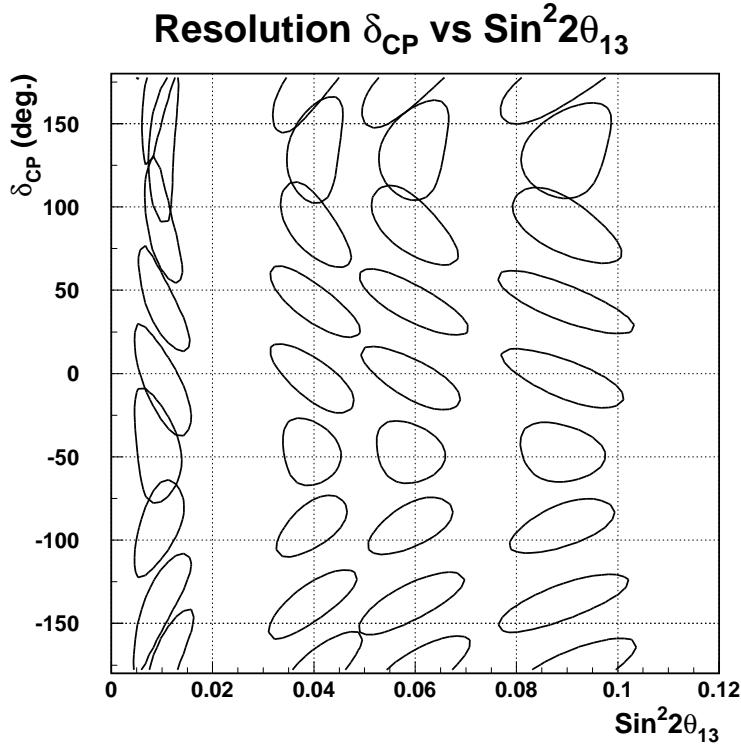
Event rate in 3 energy bins.

$$\Delta m_{21}^2 = 6 \times 10^{-5} \text{ eV}^2, \Delta m_{31}^2 = 2.5 \times 10^{-3} \text{ eV}^2$$

$$\sin^2 2\theta_{12} = 0.8, \sin^2 2\theta_{23} = 1.0$$

$$\sin^2 2\theta_{13} = 0.06$$

# Error on $\delta_{CP}$ vs $\sin^2 2\theta_{13}$

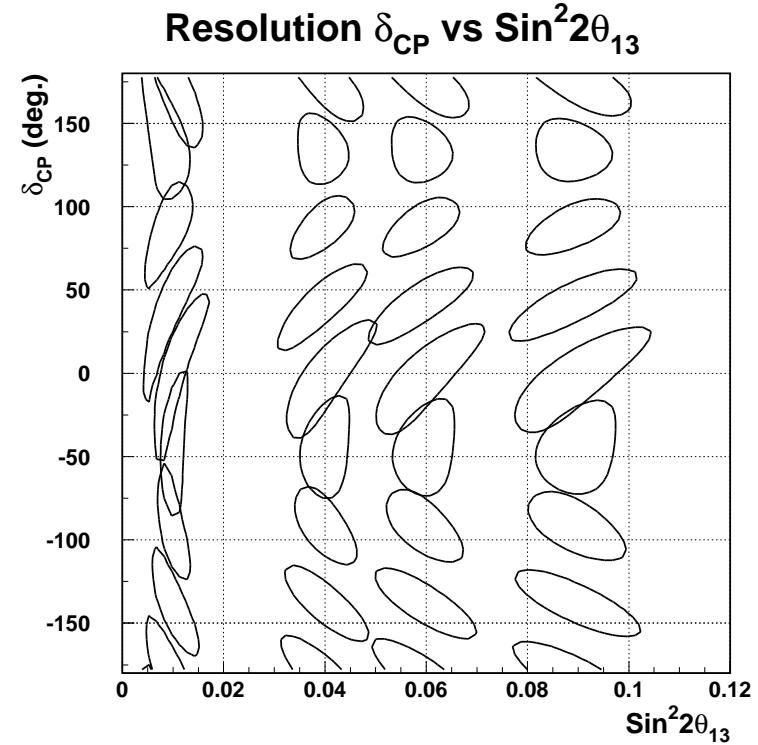
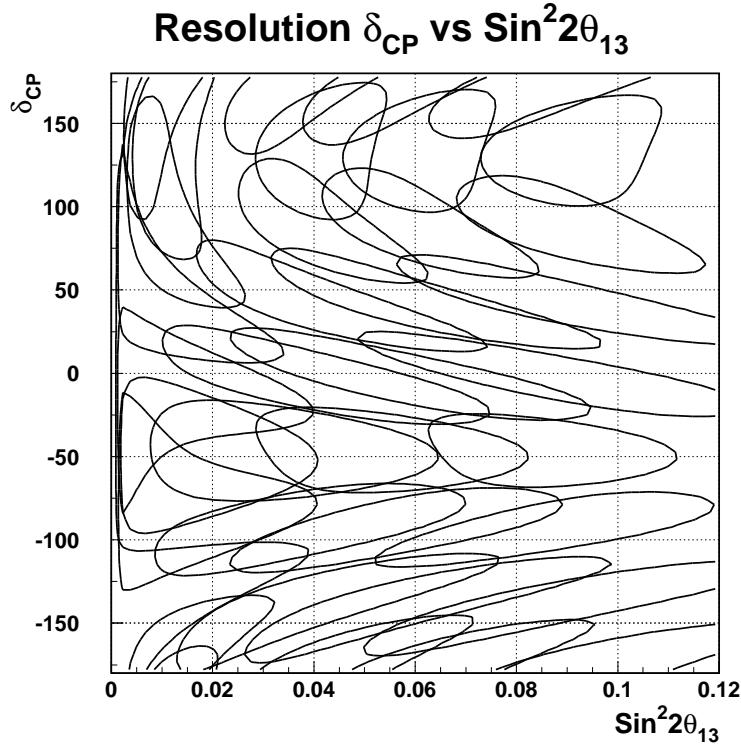


Very long baselines with a superbeam

$$\Delta m_{21}^2 = 7.3 \times 10^{-5} eV^2, \Delta m_{31}^2 = 2 \times 10^{-3} eV^2$$

$$\sin^2 2\theta_{12} = 0.86, \sin^2 2\theta_{23} = 1.0$$

# Error on $\delta_{CP}$ vs $\sin^2 2\theta_{13}$



Very long baselines with a superbeam

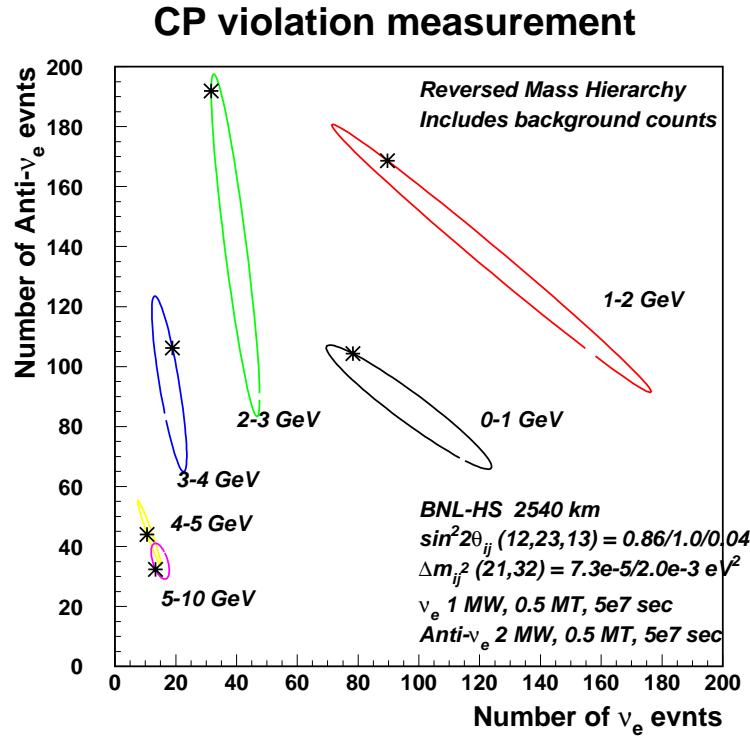
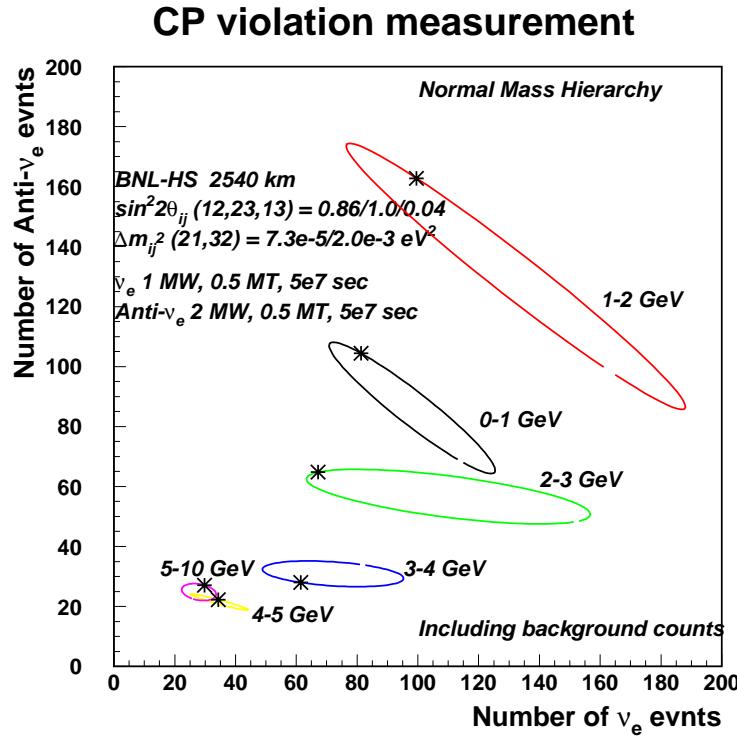
Reversed hierarchy.

$$\Delta m_{21}^2 = 7.3 \times 10^{-5} eV^2, \Delta m_{31}^2 = 2 \times 10^{-3} eV^2$$

$$\sin^2 2\theta_{12} = 0.86, \sin^2 2\theta_{23} = 1.0$$

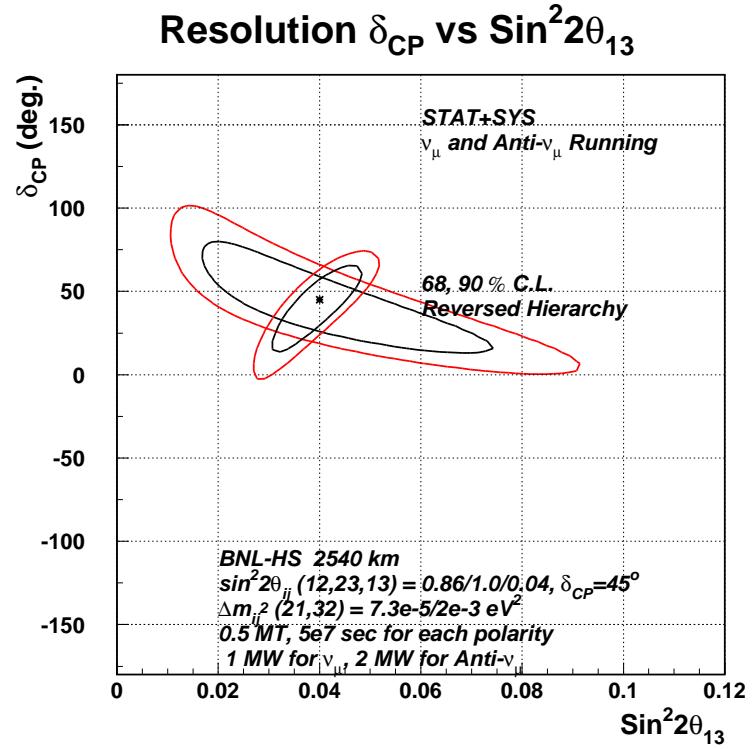
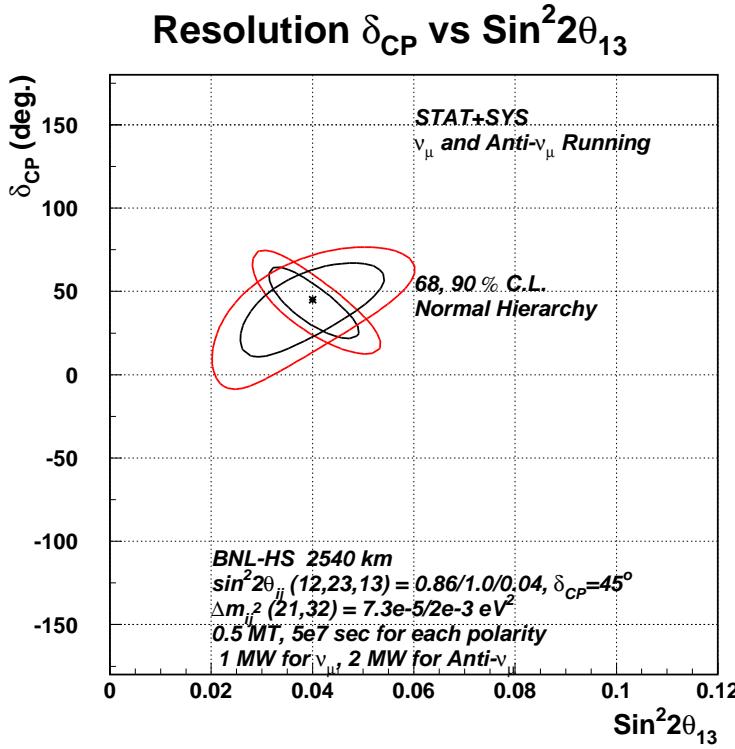
# Combining Neutrino and Antineutrino

Very long baselines with a superbeam



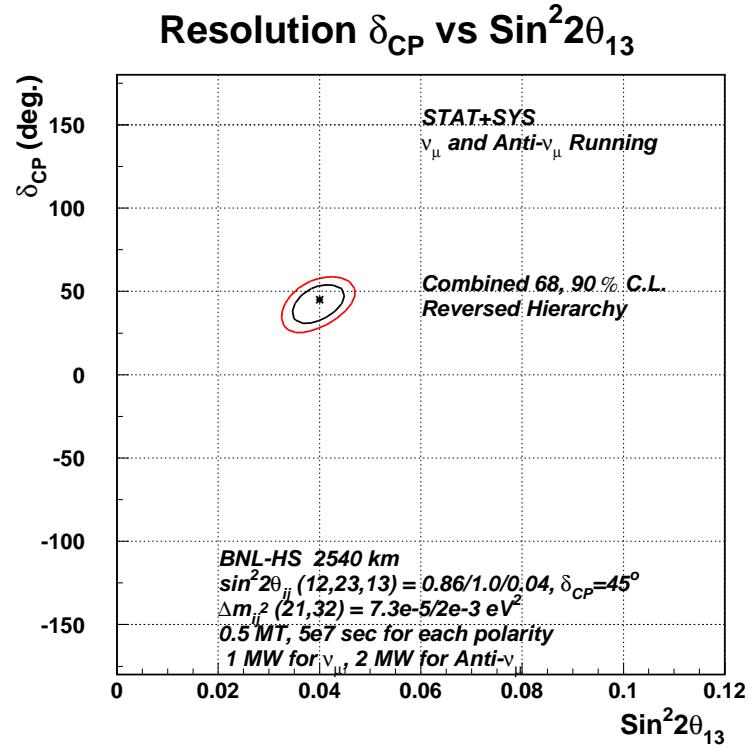
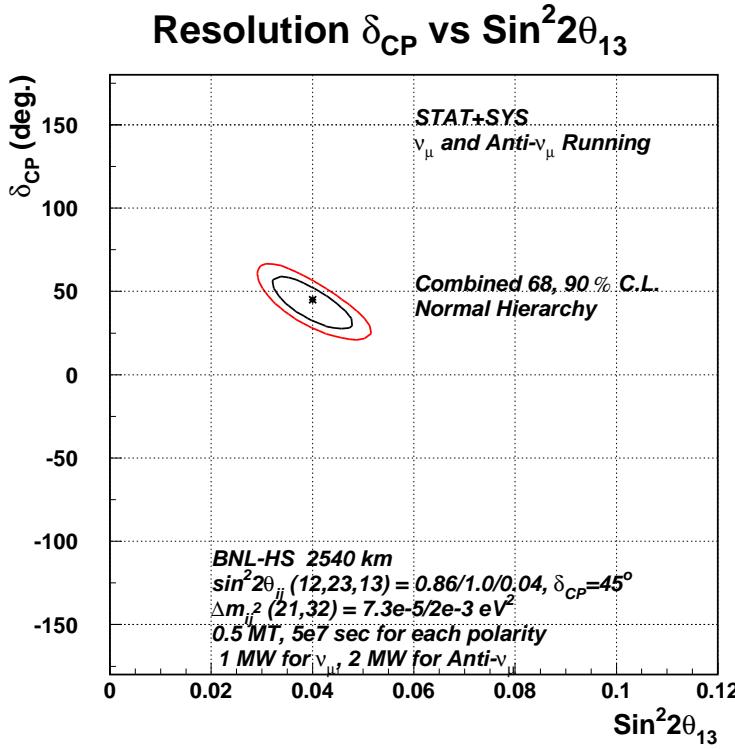
Note: No experiment can avoid matter effect. Explicit demonstration of CP violation must rely on a detailed fit to both neutrino and anti-neutrino data.

# CP with Neutrino and Antineutrino



Very long baselines with a superbeam

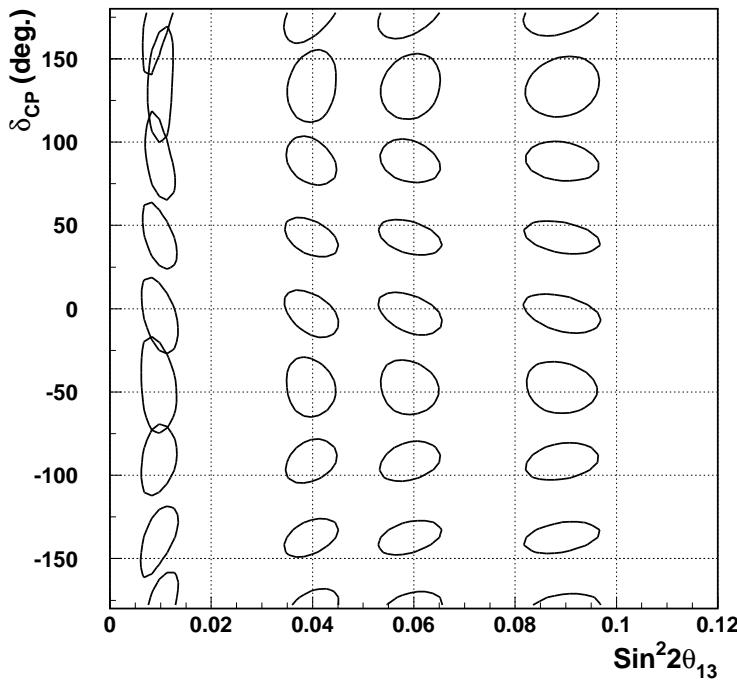
# CP with Neutrino and Antineutrino



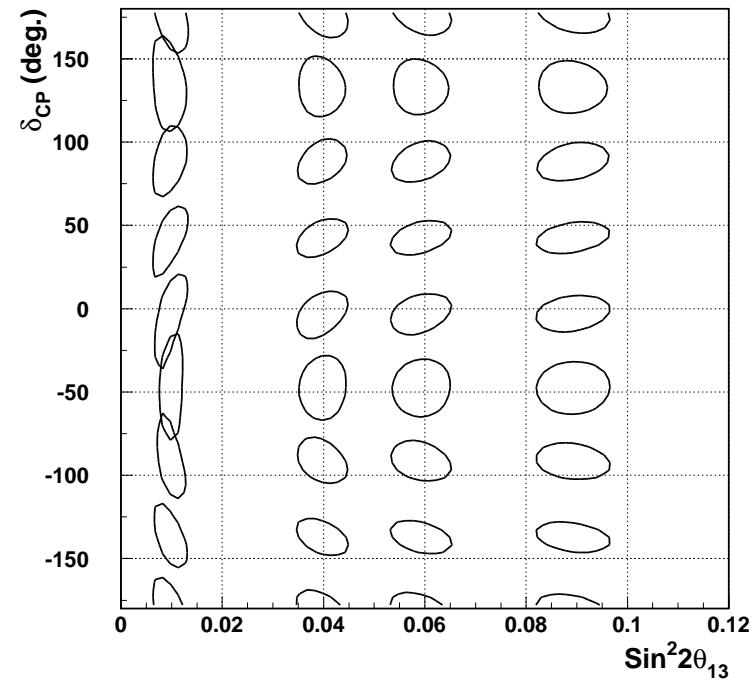
Very long baselines with a superbeam

# CP with Neutrino and Antineutrino

Regular hierarchy νν and Antivνν running

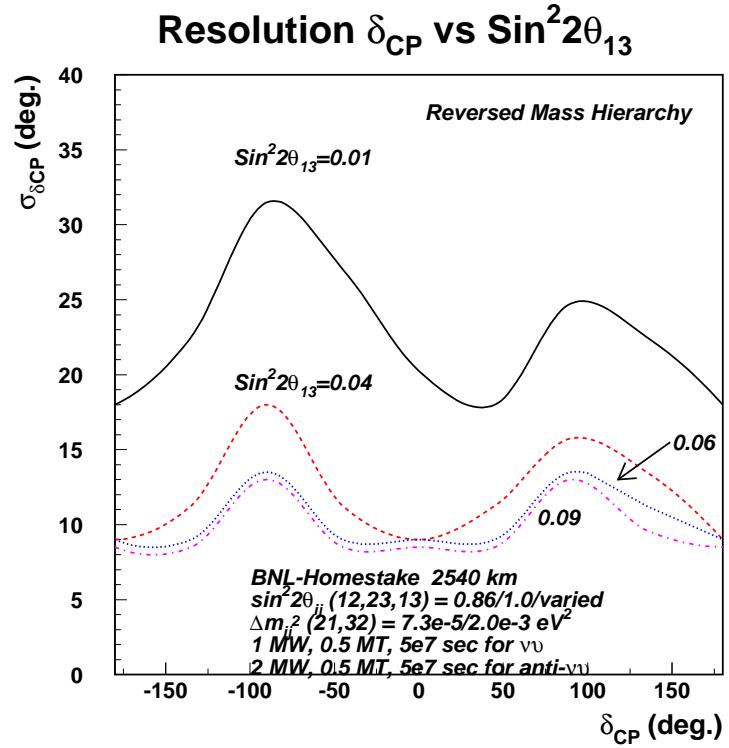
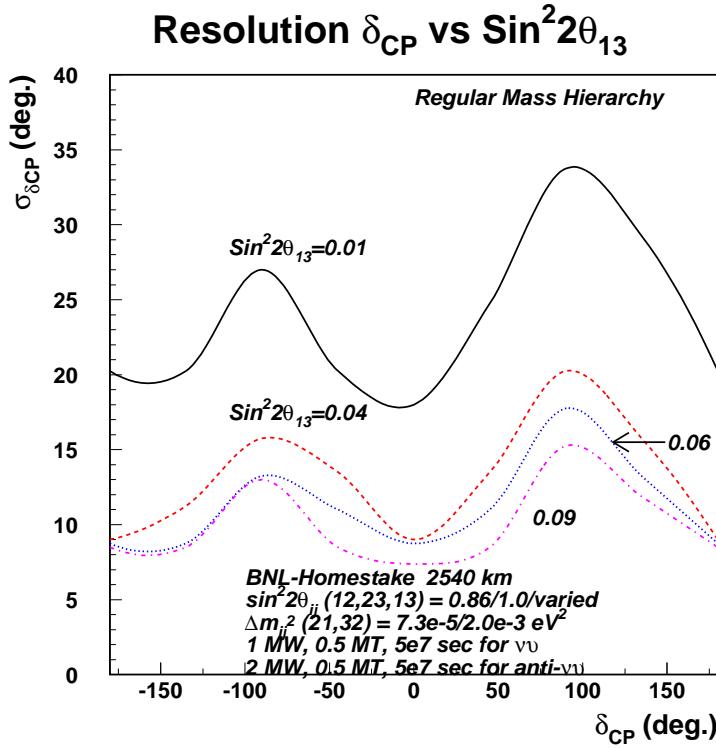


Reversed hierarchy νν and Antivνν running



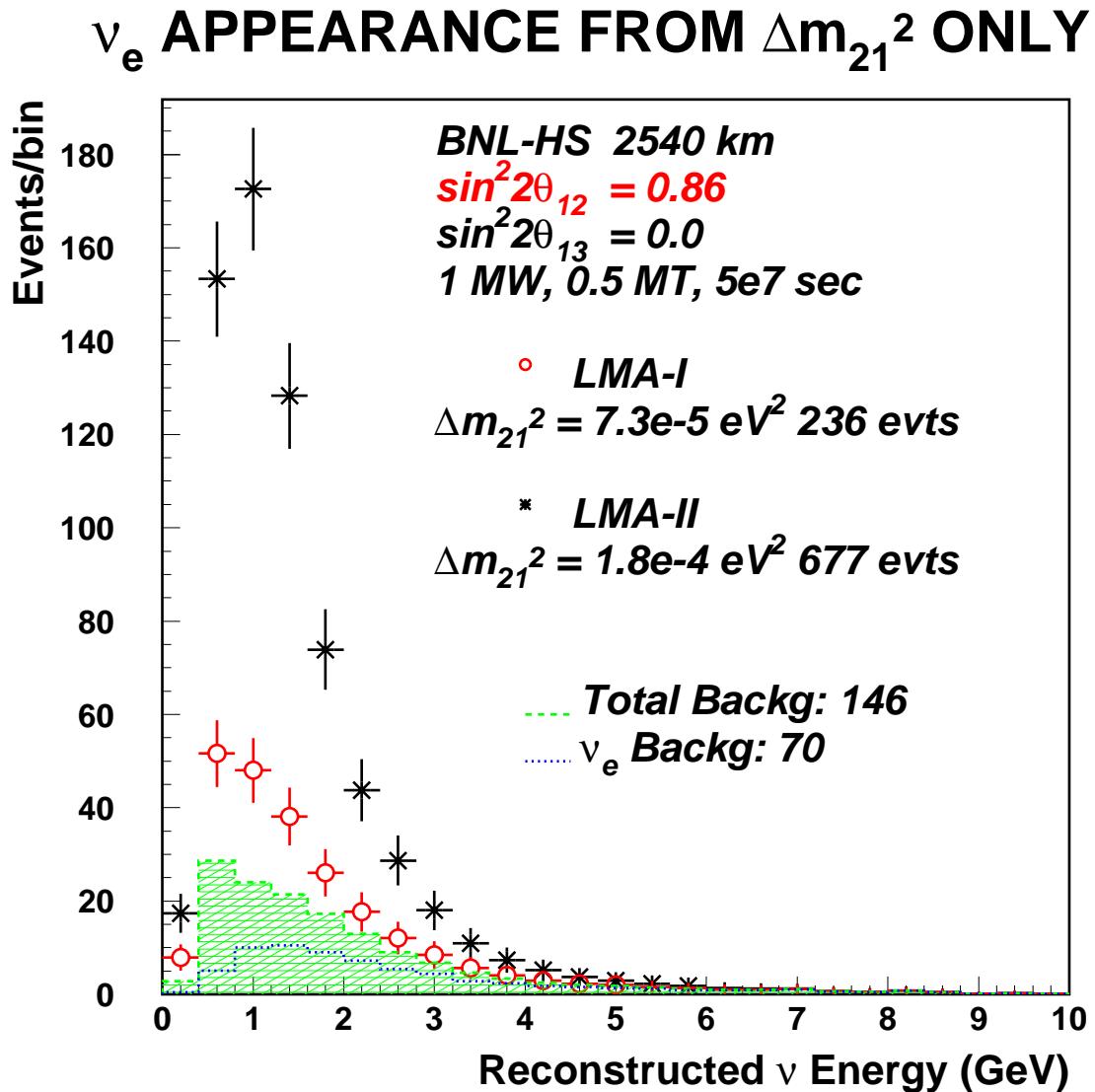
Very long baselines with a superbeam

# CP with Neutrino and Antineutrino



Very long baselines with a superbeam

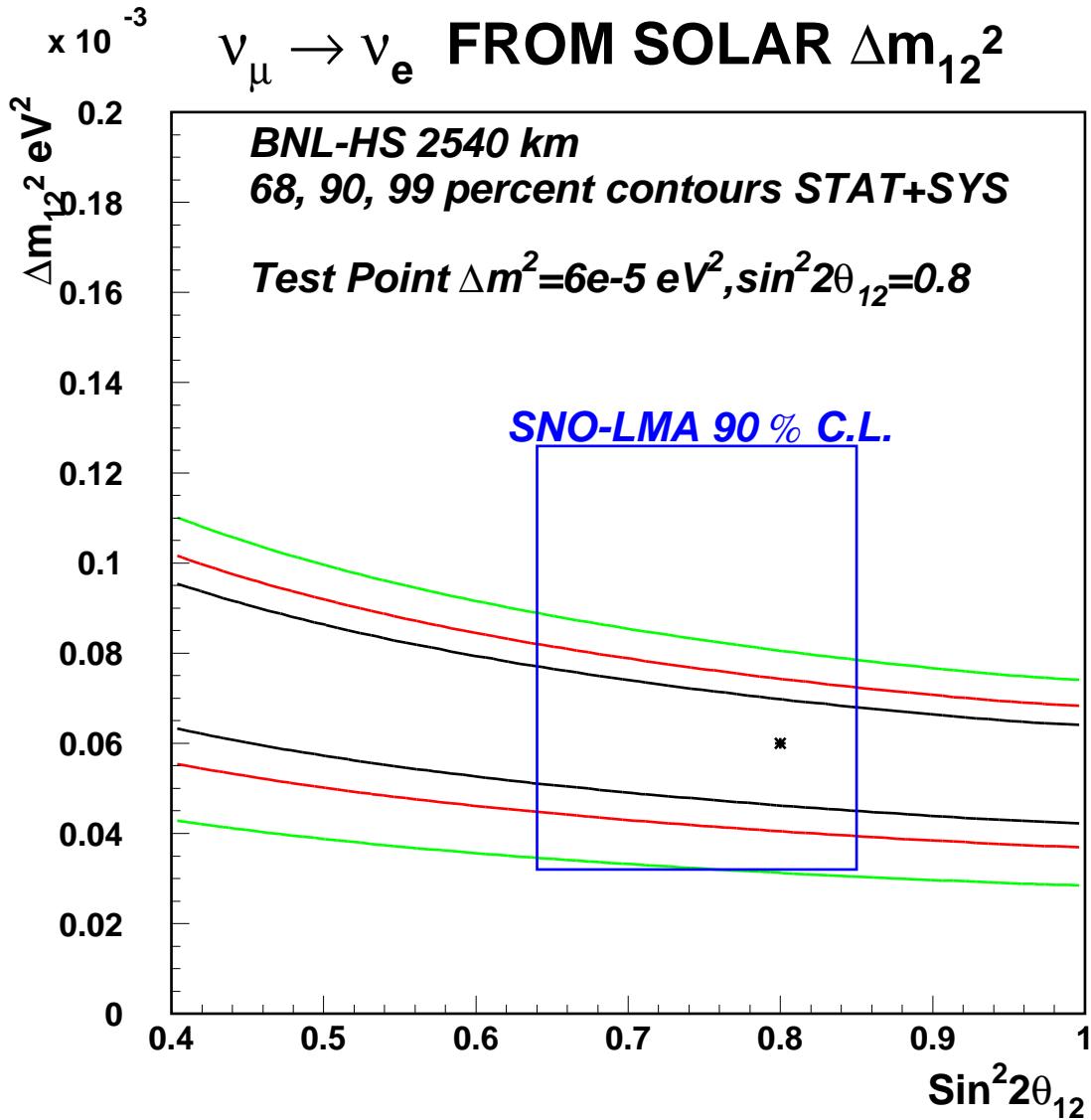
## Measurement of $\Delta m_{12}^2$



$$\theta_{13} = 0, \Delta m_{12}^2 = 7.3 \times 10^{-5} \text{ eV}^2$$

Excess of  $\sim 90$  events. Must know background

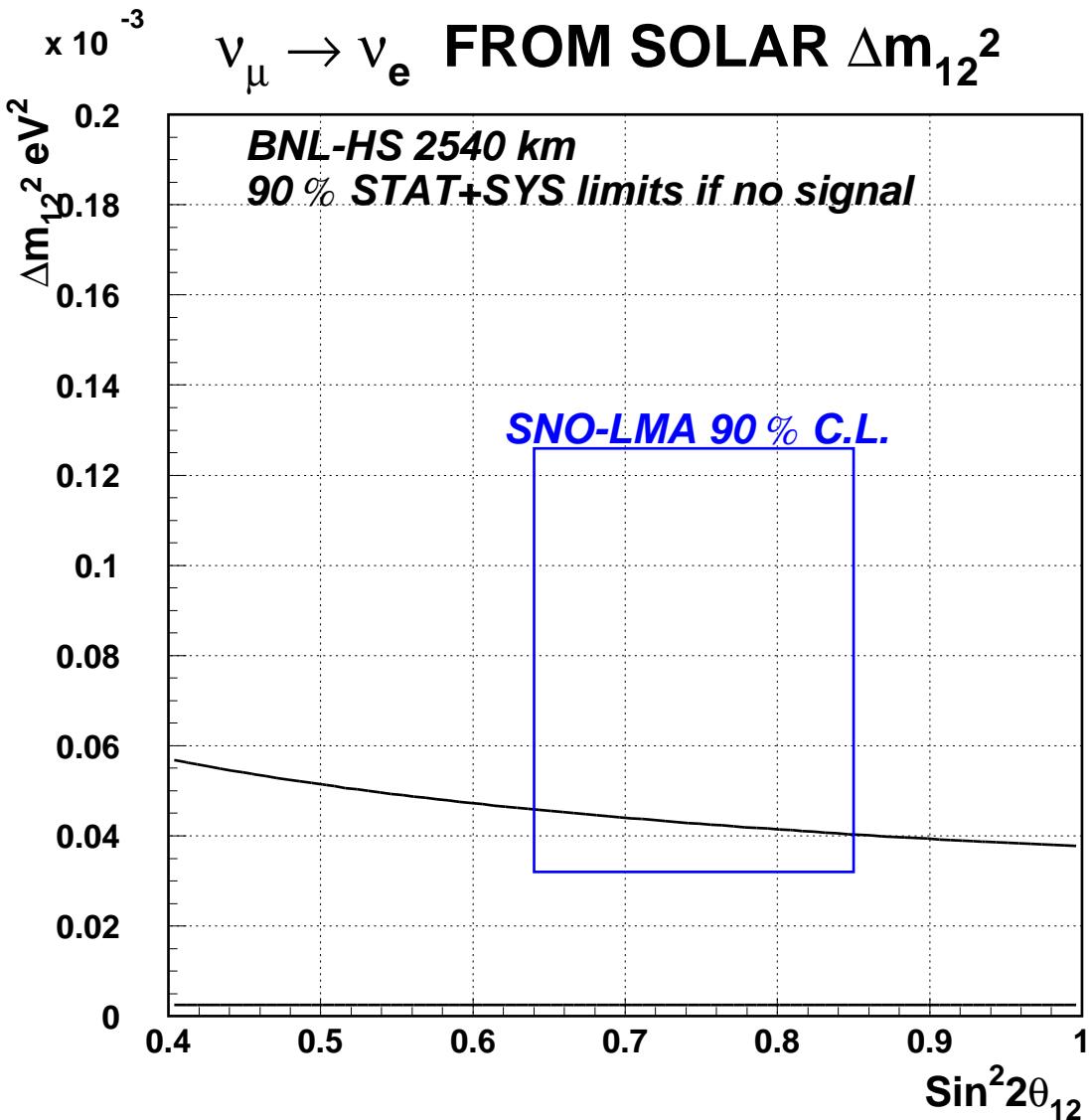
# Measurement of $\Delta m_{21}^2$



Independent  $\sim 15\%$  measurement of  $\Delta m_{21}^2$

Needs  $\sim 10\%$  error on backg.  $\Rightarrow$  near detector.

## Limit on $\Delta m_{21}^2$ vs $\sin^2 2\theta_{12}$



If no signal then a limit can be obtained that almost eliminates LMA.

## Analysis Flow Chart

How the experiment will proceed:

- After 2 years of running get a very precise measurement of  $\Delta m_{32}^2$  from disappearance and definitive signal of oscillations.
- From the measured  $\Delta m_{32}^2$  predict the shape of the electron spectrum including matter effects.
- Do we have a peak in the electron spectrum at the expected energy ? Yes No
- NO: Either  $\sin^2 2\theta_{13}$  too small or inverted mass hierarchy  $\Delta m_{32}^2 < 0$ .
  - Get an independent measurement of  $\Delta m_{21}^2$  at about  $\pm 15\%$ .
  - Run with anti-neutrinos. (next next slide)
- YES: GREAT NEWS ! GOTO NEXT SLIDE.

- YES: There is a peak in the electron spectrum from the neutrino beam.
  - Use  $\Delta m_{21}^2$  from SNO and KamLAND and make a fit to the spectrum for CP angle versus  $\sin^2 2\theta_{13}$ .
  - Accumulate more statistics and make a combined fit for  $\Delta m_{21}^2$ ,  $\delta_{CP}$  and  $\theta_{13}$ .
  - Is the CP angle too small ? NO YES
- NO: Finished ! Still run antineutrinos for more precise  $\delta_{CP}$ .
- YES: Run anti-neutrinos for more sensitivity on  $\delta_{CP}$ .  
Measure both  $\sin^2 2\theta_{13}$  and  $\delta_{CP}$

- Running with anti-neutrinos if no peak in the electron spectrum from neutrinos

Is there a peak in the electron spectrum from anti-neutrinos ? **Yes No**

- **Yes** The mass hierarchy is inverted.  
Proceed to measure  $\sin^2 2\theta_{13}$  and CP angle with anti-neutrinos.
- **No**  $\sin^2 2\theta_{13}$  is too small. Proceed to social work.

If inverted hierarchy;

measure both  $\sin^2 2\theta_{13}$  and

$\delta_{CP}$ .

OR  $\sin^2 2\theta_{13}$  is just too small for conventional beam.

## Summary of our study

- Baseline of  $> 2000$  km with wide band conventional beams are the next step in accelerator neutrino physics.
- Extraordinary, large physical effects will be seen in such an experiment.
- Very good sensitivity to neutrino properties.
  - $< 1\%$  resolution on  $\Delta m_{32}^2$
  - $< 1\%$  resolution on  $\sin^2 2\theta_{23}$
  - Sensitivity to  $\sin^2 2\theta_{13} \sim 0.005$  over a wide range of  $\Delta m_{32}^2$
  - Sensitivity to CP parameter  $\pm 25^\circ$  with neutrinos alone.
  - Sign of  $\Delta m_{32}^2$  over a wide range.
  - Measurement of  $\Delta m_{21}^2$  at  $\pm 15\%$
- The electron spectrum has a lot of physics. It can be extracted using some outside information on parameter.

# Measurement matrix

Neutrino running only; Running:  $5 \times 10^7$  sec.

Baseline: 2540 km; beam: 1 MW at 28 GeV; detector: 500 kT

	$\Delta m_{32}^2$	$\sin^2 2\theta_{23}$	$\Delta m_{21}^2$	$\sin^2 2\theta_{13}$ 90 % C.L.	$\delta_{CP}$
$\Delta m_{32}^2 > 0.001$ $\sin^2 2\theta_{13} > 0.01$	< 1%	$\sim 1\%$	$\pm 15\%$	$\pm 0.01$	$\pm 25^\circ$
$\Delta m_{32}^2 > 0.001$ $\sin^2 2\theta_{13} < 0.01$	< 1%	$\sim 1\%$	$\pm 15\%$	Limit $< 0.005$	No Measure.

Not complete story, but an impression. Assume  $m_3 > m_2 > m_1$ .

Need good energy calibration for  $\Delta m_{32}^2$  ( $\sim 100 MeV$  LINAC ?)

Need small error on backg. for  $\Delta m_{21}^2$  and CP. (Near Detector)

## Some comments on detector

- Detector studies have started. Need more manpower.
- Water Cherenkov
  - 50 kT SuperK is existence proof.
  - Background rejection ? need another  $\times 3$  to 5 to reach level in this talk.
  - Additional imaging capability ?
- Liquid Argon TPC
  - 100 kT module never built.
  - Current size 300Ton.
  - Needs detailed simulations.
- Any other technology ?

## What is Next ?

White paper: hep-ex/0211001

Short paper: hep-ph/0303081, published PRD68,  
012002, 2003

Can we use events such as  $\nu_e + N \rightarrow e^- + \pi^+ + N$  ?

Background determination with near det.

- The experiment is technically feasible.  
Direct costs.

AGS upgrade, Hill, Proton transp., horns,  
decay tunnel:  $\sim \$150M$

This can be a staged program that starts  
with \$90 M at the AGS and \$150 M at  
Homestake for first critical results.

- The detector has applications far beyond  
accelerator neutrinos. And should have a very  
diverse and rich physics program.  
Detector: \$300 M for 10% PMT coverage ?  
If water Cherenkov cannot have the needed  
performance then what ?

## **Very long baselines with a superbeam**

Two possibilities

- 1) Increase AGS to 2 MW by going to 5 Hz operation
- 2) Make finer grain detector at 100 kT. Use all events.

Optimization of the detector and accelerator needs much more detailed simulation study.